The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

MATHEMATICS B

Tuesday, August 13, 2002 — 8:30 to 11:30 a.m., only

Print Your Name:				
Print Your School's	Name:	 	 	

Print your name and the name of your school in the boxes above. Then turn to the last page of this booklet, which is the answer sheet for Part I. Fold the last page along the perforations and, slowly and carefully, tear off the answer sheet. Then fill in the heading of your answer sheet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. Any work done on this sheet of scrap graph paper will *not* be scored. All work should be written in pen, except graphs and drawings, which should be done in pencil.

This examination has four parts, with a total of 34 questions. You must answer all questions in this examination. Write your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. The formulas that you may need to answer some questions in this examination are found on page 2.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice. . .

A graphing calculator, a straightedge (ruler), and a compass must be available for your use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

Formulas

Area of Triangle

 $K = \frac{1}{2}ab \sin C$

Functions of the Sum of Two Angles

sin (A + B) = sin A cos B + cos A sin Bcos (A + B) = cos A cos B - sin A sin B

Functions of the Difference of Two Angles

 $\sin (A - B) = \sin A \cos B - \cos A \sin B$ $\cos (A - B) = \cos A \cos B + \sin A \sin B$

Law of Sines

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Law of Cosines

 $a^2 = b^2 + c^2 - 2bc \cos A$

Functions of the Double Angle

 $\sin 2A = 2 \sin A \cos A$ $\cos 2A = \cos^2 A - \sin^2 A$ $\cos 2A = 2 \cos^2 A - 1$ $\cos 2A = 1 - 2 \sin^2 A$

Functions of the Half Angle

$$\sin \frac{1}{2}A = \pm \sqrt{\frac{1 - \cos A}{2}}$$
$$\cos \frac{1}{2}A = \pm \sqrt{\frac{1 + \cos A}{2}}$$



Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Record your answers in the spaces provided on the separate answer sheet. [40]

1 Which fraction represents the probability of obtaining *exactly* eight heads in ten tosses of a fair coin?

Use this space for computations.

$\frac{45}{1,024}$	(3)	$\frac{90}{1,024}$
	$\frac{45}{1,024}$	$\frac{45}{1,024}$ (3)

- (2) $\frac{64}{1,024}$ (4) $\frac{180}{1,024}$
- 2 In a New York City high school, a survey revealed the mean amount of cola consumed each week was 12 bottles and the standard deviation was 2.8 bottles. Assuming the survey represents a normal distribution, how many bottles of cola per week will approximately 68.2% of the students drink?

(1)	6.4 to 12	(3)	9.2 to 14.8
(2)	6.4 to 17.6	(4)	12 to 20.4

- **3** What is the solution of the inequality $|x + 3| \le 5$?
 - (1) $-8 \le x \le 2$ (2) $-2 \le x \le 8$ (3) $x \le -8$ or $x \ge 2$ (4) $x \le -2$ or $x \ge 8$
- **4** What is the domain of $f(x) = 2^x$?
 - (1) all integers (3) $x \ge 0$
 - (2) all real numbers (4) $x \le 0$
- **5** A function is defined by the equation y = 5x 5. Which equation defines the inverse of this function?

(1) $y = \frac{1}{5x - 5}$	(3) $x = \frac{1}{5y - 5}$
(2) $y = 5x + 5$	(4) $x = 5y - 5$

6 An architect is designing a building to include an arch in the shape of a semi-ellipse (half an ellipse), such that the width of the arch is 20 feet and the height of the arch is 8 feet, as shown in the accompanying diagram.

Use this space for computations.



Which equation models this arch?

- (1) $\frac{x^2}{100} + \frac{y^2}{64} = 1$ (3) $\frac{x^2}{64} + \frac{y^2}{100} = 1$ (2) $\frac{x^2}{400} + \frac{y^2}{64} = 1$ (4) $\frac{x^2}{64} + \frac{y^2}{400} = 1$
- 7 To balance a seesaw, the distance, in feet, a person is from the fulcrum is inversely proportional to the person's weight, in pounds. Bill, who weighs 150 pounds, is sitting 4 feet away from the fulcrum. If Dan weighs 120 pounds, how far from the fulcrum should he sit to balance the seesaw?

(1)	4.5 ft	(3)	3 ft
(2)	3.5 ft	(4)	$5 {\rm ft}$

8 What is the *last* term in the expansion of $(x + 2y)^5$?

(1)	y^5	(3)	$10y^{5}$
(2)	$2y^5$	(4)	$32y^{5}$

9 In the equation $\log_x 4 + \log_x 9 = 2$, *x* is equal to

- (1) $\sqrt{13}$ (3) 6.5
- (2) 6 (4) 18

10 Which expression represents the sum of $\frac{1}{\sqrt{3}}$ and $\frac{1}{\sqrt{2}}$?

- (1) $\frac{2\sqrt{3}+3\sqrt{2}}{6}$ (3) $\frac{\sqrt{3}+\sqrt{2}}{3}$
- (2) $\frac{2}{\sqrt{5}}$ (4) $\frac{\sqrt{3}+\sqrt{2}}{2}$

11 Which equation has imaginary roots?

(1) $x^2 - 1 = 0$ (2) $x^2 - 2 = 0$ (3) $x^2 + x + 1 = 0$ (4) $x^2 - x - 1 = 0$

12 If $\log k = c \log v + \log p$, k equals

13 If ${}_{n}C_{r}$ represents the number of combinations of *n* items taken *r* at a

time, what is the value of $\sum_{r=1}^{3} {}_{4}C_{r}$?

- (1) 24 (3) 6
- (2) 14 (4) 4

Use this space for computations.

14 In the accompanying diagram of $\triangle ABC$, m $\angle A = 30$, m $\angle C = 50$, and AC = 13.

Use this space for computations.



What is the length of side \overline{AB} to the *nearest tenth*?

- $(1) \ 6.6 \qquad (3) \ 11.5$
- (2) 10.1 (4) 12.0

15 Expressed in simplest form, $i^{16} + i^6 - 2i^5 + i^{13}$ is equivalent to

- (1) 1 (3) i
- (2) -1 (4) -i

16 If point (a,b) lies on the graph y = f(x), the graph $y = f^{-1}(x)$ must contain point

- (1) (b,a) (3) (0,b)
- (2) (a,0) (4) (-a,-b)

17 If the sum of the roots of $x^2 + 3x - 5 = 0$ is added to the product of its roots, the result is

18 The expression
$$\frac{3^{\frac{1}{3}}}{3^{\frac{2}{3}}}$$
 is equivalent to
(1) 1 (3) 3
(2) $\sqrt{3}$ (4) $\frac{1}{\sqrt[3]{3}}$

19 The accompanying graph represents the figure [.

y ↓ ↓ ↓ ↓ ↓ ↓ Use this space for computations.





20 Which expression is equivalent to the complex fraction $\frac{\frac{x}{x+2}}{1-\frac{x}{x+2}}$?

(1)
$$\frac{2}{x}$$
 (3) $\frac{2x}{x+2}$

(2)
$$\frac{x}{2}$$
 (4) $\frac{2x}{x^2+4}$

Part II

Answer all questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

21 A used car was purchased in July 1999 for \$11,900. If the car depreciates 13% of its value each year, what is the value of the car, to the *nearest hundred dollars*, in July 2002?

22 The amount of time that a teenager plays video games in any given week is normally distributed. If a teenager plays video games an average of 15 hours per week, with a standard deviation of 3 hours, what is the probability of a teenager playing video games between 15 and 18 hours a week?

23 An art student wants to make a string collage by connecting six equally spaced points on the circumference of a circle to its center with string. What would be the radian measure of the angle between two adjacent pieces of string, in simplest form?

24 The Franklins inherited \$3,500, which they want to invest for their child's future college expenses. If they invest it at 8.25% with interest compounded monthly, determine the value of the account, in dollars, after 5 years. Use the formula $A = P(1 + \frac{r}{n})^{nt}$, where A = value of the investment after t years, P = principal invested, r = annual interest rate, and n = number of times compounded per year.

25	A toy truck is located within a circular play area. Alex and Dominic are sitting on opposite endpoints of a chord that contains the truck. Alex is 4 feet from the truck, and Dominic is 3 feet from the truck. Meira and Tamara are sitting on opposite endpoints of another chord containing the truck. Meira is 8 feet from the truck. How many feet, to the <i>nearest tenth of a foot</i> , is Tamara from the truck? Draw a dia- gram to support your answer.
26	Two sides of a triangular-shaped pool measure 16 feet and 21 feet, and the included angle measures 58°. What is the area, to the <i>nearest</i> <i>tenth of a square foot</i> , of a nylon cover that would exactly cover the surface of the pool?

Part III

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [24]

27 The cost (C) of selling x calculators in a store is modeled by the	
equation $C = \frac{3,200,000}{x} + 60,000$. The store profit (P) for these sales is	
modeled by the equation $P = 500x$. What is the minimum number of	
calculators that have to be sold for profit to be greater than cost?	

28 Two tow trucks try to pull a car out of a ditch. One tow truck applies a force of 1,500 pounds while the other truck applies a force of 2,000 pounds. The resultant force is 3,000 pounds. Find the angle between the two applied forces, rounded to the *nearest degree*.

29 A rock is thrown vertically from the ground with a velocity of 24 meters per second, and it reaches a height of $2 + 24t - 4.9t^2$ after t seconds. How many seconds after the rock is thrown will it reach maximum height, and what is the maximum height the rock will reach, in meters? How many seconds after the rock is thrown will it hit the ground? Round your answers to the *nearest hundredth*. [Only an algebraic or graphic solution will be accepted.]





32 The breaking strength, y, in tons, of steel cable with diameter d, in inches, is given in the table below.

d (in)	0.50	0.75	1.00	1.25	1.50	1.75	
y (tons)	9.85	21.80	38.30	59.20	84.40	114.00	

On the accompanying grid, make a scatter plot of these data. Write the exponential regression equation, expressing the regression coefficients to the *nearest tenth*.



Part IV

Answer all questions in this part. Each correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [12]

33 Carmen and Jamal are standing 5,280 feet apart on a straight, horizontal road. They observe a hot-air balloon between them directly above the road. The angle of elevation from Carmen is 60° and from Jamal is 75° . Draw a diagram to illustrate this situation and find the height of the balloon to the *nearest foot*. **34** Electrical circuits can be connected in series, one after another, or in parallel circuits that branch off a main line. If circuits are hooked up in parallel, the reciprocal of the total resistance in the series is found by adding the reciprocals of each resistance, as shown in the accompanying diagram.



If $R_1 = x$, $R_2 = x + 3$, and the total resistance, R_T , is 2.25 ohms, find the positive value of R_1 to the *nearest tenth of an ohm*.



Scrap Graph Paper — This sheet will *not* be scored.

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Tear Here

Scrap Graph Paper — This sheet will *not* be scored.



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	Tea	cher	•••	 	
					Your a
	1			 	
	2			 	
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	5			 	

Your answers for Parts II, III, and IV should be written in the test booklet.

The declaration below should be signed when you have completed the examination.

I do hereby affirm, at the close of this examination, that I had no unlawful knowledge of the questions or answers prior to the examination and that I have neither given nor received assistance in answering any of the questions during the examination.

Signature

Math. B - Aug. '02

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MATHEMATICS B

Tuesday, August 13, 2002 — 8:30 to 11:30 a.m., only

ANSWER SHEET

Student	 Sex:	\Box Male	\Box Female	Grade	
Teacher	 Schoo	ol			

answers to Part I should be recorded on this answer sheet.

Part I

Answer all 20 questions in this part.

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		MATH	EMATICS	В	
Questi	on	Maximum Credit	Credits Earned	Rater's/Scorer's Initials	
Part I 1	-20	40			
Part II	21	2			
	22	2			
	23	2			
	24	2			
	25	2			
	26	2			
Part III	27	4			
	28	4			
	29	4			
	30	4			
	31	4			
	32	4			
Part IV	33	6			
	34	6			
Maximu Total	ım	88			
			Total Raw Score	Checked by	

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Notes to raters. . .

- Each paper should be scored by a minimum of three raters.
- The table for converting the total raw score to the scaled score is provided in the scoring key for this examination.The scaled score is the student's final examination score.