

FOR TEACHERS ONLY

The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

GEOMETRY

Tuesday, January 26, 2016 — 1:15 to 4:15 p.m., only

SCORING KEY AND RATING GUIDE

Mechanics of Rating

The following procedures are to be followed for scoring student answer papers for the Regents Examination in Geometry. More detailed information about scoring is provided in the publication *Information Booklet for Scoring the Regents Examinations in Mathematics*.

Do *not* attempt to correct the student's work by making insertions or changes of any kind. In scoring the open-ended questions, use check marks to indicate student errors. Unless otherwise specified, mathematically correct variations in the answers will be allowed. Units need not be given when the wording of the questions allows such omissions.

Each student's answer paper is to be scored by a minimum of three mathematics teachers. No one teacher is to score more than approximately one-third of the open-ended questions on a student's paper. Teachers may not score their own students' answer papers. On the student's separate answer sheet, for each question, record the number of credits earned and the teacher's assigned rater/scorer letter.

Schools are not permitted to rescore any of the open-ended questions on this exam after each question has been rated once, regardless of the final exam score. Schools are required to ensure that the raw scores have been added correctly and that the resulting scale score has been determined accurately.

Raters should record the student's scores for all questions and the total raw score on the student's separate answer sheet. Then the student's total raw score should be converted to a scale score by using the conversion chart that will be posted on the Department's web site at: <http://www.p12.nysed.gov/assessment/> on Tuesday, January 26, 2016. Because scale scores corresponding to raw scores in the conversion chart may change from one administration to another, it is crucial that, for each administration, the conversion chart provided for that administration be used to determine the student's final score. The student's scale score should be entered in the box provided on the student's separate answer sheet. The scale score is the student's final examination score.

If the student’s responses for the multiple-choice questions are being hand scored prior to being scanned, the scorer must be careful not to make any marks on the answer sheet except to record the scores in the designated score boxes. Marks elsewhere on the answer sheet will interfere with the accuracy of the scanning.

Part I

Allow a total of 56 credits, 2 credits for each of the following. Allow credit if the student has written the correct answer instead of the numeral 1, 2, 3, or 4.

| | | |
|----------------------------|----------------------------|----------------------------|
| (1) 2 | (11) 1 | (21) 4 |
| (2) 2 | (12) 3 | (22) 1 |
| (3) 3 | (13) 4 | (23) 1 |
| (4) 4 | (14) 1 | (24) 2 |
| (5) 1 | (15) 3 | (25) 4 |
| (6) 2 | (16) 2 | (26) 4 |
| (7) 4 | (17) 2 | (27) 3 |
| (8) 3 | (18) 2 | (28) 2 |
| (9) 2 | (19) 1 | |
| (10) 3 | (20) 3 | |

Updated information regarding the rating of this examination may be posted on the New York State Education Department’s web site during the rating period. Check this web site at: <http://www.p12.nysed.gov/assessment/> and select the link “Scoring Information” for any recently posted information regarding this examination. This site should be checked before the rating process for this examination begins and several times throughout the Regents Examination period.

Beginning in June 2013, the Department is providing supplemental scoring guidance, the “Sample Response Set,” for the Regents Examination in Geometry. This guidance is not required as part of the scorer training. It is at the school’s discretion to incorporate it into the scorer training or to use it as supplemental information during scoring. While not reflective of all scenarios, the sample student responses selected for the Sample Response Set illustrate how less common student responses to open-ended questions may be scored. The Sample Response Set will be available on the Department’s web site at: <http://www.nysedregents.org/Geometry/>.

General Rules for Applying Mathematics Rubrics

I. General Principles for Rating

The rubrics for the constructed-response questions on the Regents Examination in Geometry are designed to provide a systematic, consistent method for awarding credit. The rubrics are not to be considered all-inclusive; it is impossible to anticipate all the different methods that students might use to solve a given problem. Each response must be rated carefully using the teacher's professional judgment and knowledge of mathematics; all calculations must be checked. The specific rubrics for each question must be applied consistently to all responses. In cases that are not specifically addressed in the rubrics, raters must follow the general rating guidelines in the publication *Information Booklet for Scoring the Regents Examinations in Mathematics*, use their own professional judgment, confer with other mathematics teachers, and/or contact the State Education Department for guidance. During each Regents Examination administration period, rating questions may be referred directly to the Education Department. The contact numbers are sent to all schools before each administration period.

II. Full-Credit Responses

A full-credit response provides a complete and correct answer to all parts of the question. Sufficient work is shown to enable the rater to determine how the student arrived at the correct answer.

When the rubric for the full-credit response includes one or more examples of an acceptable method for solving the question (usually introduced by the phrase “such as”), it does not mean that there are no additional acceptable methods of arriving at the correct answer. Unless otherwise specified, mathematically correct alternative solutions should be awarded credit. The only exceptions are those questions that specify the type of solution that must be used; e.g., an algebraic solution or a graphic solution. A correct solution using a method other than the one specified is awarded half the credit of a correct solution using the specified method.

III. Appropriate Work

Full-Credit Responses: The directions in the examination booklet for all the constructed-response questions state: “Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc.” The student has the responsibility of providing the correct answer **and** showing how that answer was obtained. The student must “construct” the response; the teacher should not have to search through a group of seemingly random calculations scribbled on the student paper to ascertain what method the student may have used.

Responses With Errors: Rubrics that state “Appropriate work is shown, but...” are intended to be used with solutions that show an essentially complete response to the question but contain certain types of errors, whether computational, rounding, graphing, or conceptual. If the response is incomplete; i.e., an equation is written but not solved or an equation is solved but not all of the parts of the question are answered, appropriate work has **not** been shown. Other rubrics address incomplete responses.

IV. Multiple Errors

Computational Errors, Graphing Errors, and Rounding Errors: Each of these types of errors results in a 1-credit deduction. Any combination of two of these types of errors results in a 2-credit deduction. No more than 2 credits should be deducted for such mechanical errors in any response. The teacher must carefully review the student's work to determine what errors were made and what type of errors they were.

Conceptual Errors: A conceptual error involves a more serious lack of knowledge or procedure. Examples of conceptual errors include using the incorrect formula for the area of a figure, choosing the incorrect trigonometric function, or multiplying the exponents instead of adding them when multiplying terms with exponents.

If a response shows repeated occurrences of the same conceptual error, the student should not be penalized twice. If the same conceptual error is repeated in responses to other questions, credit should be deducted in each response.

For 4- and 6-credit questions, if a response shows one conceptual error and one computational, graphing, or rounding error, the teacher must award credit that takes into account both errors. Refer to the rubric for specific scoring guidelines.

Part II

For each question, use the specific criteria to award a maximum of 2 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

(29) [2] 16, and correct work is shown.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] A correct proportion is written, but no further correct work is shown.

or

[1] 16, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(30) [2] $\triangle A'B'C'$ is graphed and labeled correctly.

[1] Appropriate work is shown, but one graphing error is made.

or

[1] Appropriate work is shown, but one conceptual error is made, such as a dilation of 2.

or

[1] The image of $\triangle ABC$ is graphed correctly, but it is not labeled or is labeled incorrectly.

or

[1] $A'(3, -2)$, $B'(0,1)$, and $C'(3,1)$ are stated, but no further correct work is shown.

[0] $(3, -2)$, $(0,1)$, and $(3,1)$ are stated, but are not labeled or are labeled incorrectly.

or

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(31) [2] 21.5, and correct work is shown.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] 21.5, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(32) [2] 17 or $\sqrt{289}$, and correct work is shown.

[1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] 17, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (33) [2] 160, and correct work is shown.
- [1] Appropriate work is shown, but one computational error is made.
- or***
- [1] Appropriate work is shown, but one conceptual error is made.
- or***
- [1] 160, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (34) [2] A correct construction is drawn showing all appropriate arcs, and the angle bisector is drawn.
- [1] A correct construction for an angle bisector is drawn for an angle other than $\angle D$.
- or***
- [1] All construction arcs are drawn, but the angle bisector is not drawn.
- [0] A drawing that is not an appropriate construction is shown.
- or***
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
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Part III

For each question, use the specific criteria to award a maximum of 4 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

(35) [4] $\triangle A'B'C'$ and $\triangle A''B''C''$ are graphed and labeled correctly, and a rotation of 180° or a reflection through the origin is stated.

[3] Appropriate work is shown, but one computational, graphing, or labeling error is made.

or

[3] $\triangle A'B'C'$ and $\triangle A''B''C''$ are graphed and labeled correctly, but a single transformation is not stated or is stated incorrectly.

[2] Appropriate work is shown, but two or more computational, graphing, or labeling errors are made.

or

[2] Appropriate work is shown, but one conceptual error is made.

or

[2] $\triangle A'B'C'$ and $\triangle A''B''C''$ are graphed correctly, but are not labeled or are labeled incorrectly. No further correct work is shown.

[1] Appropriate work is shown, but one conceptual error and one computational, graphing, or labeling error are made.

or

[1] $\triangle A'B'C'$ is graphed and labeled correctly, but no further correct work is shown.

or

[1] Appropriate work is shown to find $A''(-2, -5)$, $B''(-5, -7)$, and $C''(-4, -1)$, but no graphs are shown.

or

[1] A rotation of 180° or a reflection through the origin is stated, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (36) [4] Both equations are graphed correctly, and $(-3, -1)$ and $(1, 7)$ are stated.
- [3] Appropriate work is shown, but one computational or graphing error is made.
- or***
- [3] Both equations are graphed correctly, but only $(-3, -1)$ or $(1, 7)$ is stated.
- [2] Appropriate work is shown, but two or more computational or graphing errors are made.
- or***
- [2] Appropriate work is shown, but one conceptual error is made.
- or***
- [2] Both equations are graphed correctly, but the points of intersection are not stated or are stated incorrectly.
- or***
- [2] Appropriate work is shown to find $(-3, -1)$ and $(1, 7)$, but a method other than graphing is used.
- [1] Appropriate work is shown, but one conceptual error and one computational or graphing error are made.
- or***
- [1] One equation is graphed correctly, but no further correct work is shown.
- or***
- [1] $(-3, -1)$ and $(1, 7)$ are stated, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (37) [4] A complete and correct proof that includes a concluding statement is written.
- [3] A proof is written that includes a concluding statement, but one computational or graphing error is made.
- or**
- [3] A proof is written that includes a concluding statement, but one reason is missing.
- or**
- [3] Appropriate work is shown to prove $\angle RST$ is a right angle, but a concluding statement is missing or is incorrect.
- or**
- [3] Appropriate work is shown to demonstrate that the Pythagorean Theorem is satisfied, but a concluding statement is missing or is incorrect.
- [2] A proof is written that includes a concluding statement, but two or more computational or graphing errors are made.
- or**
- [2] Appropriate work is shown, but one conceptual error is made.
- or**
- [2] Appropriate work is shown to prove $\overline{RS} \perp \overline{ST}$, but no further correct work is shown.
- or**
- [2] A correct substitution is made into the Pythagorean Theorem, but no further correct work is shown.
- [1] A proof is written, but one conceptual error and one computational or graphing error are made.
- or**
- [1] Appropriate work is shown to find the lengths of all three sides, but no further correct work is shown.
- or**
- [1] Appropriate work is shown to find the slopes of \overline{RS} and \overline{ST} , but no further correct work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
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Part IV

For this question, use the specific criteria to award a maximum of 6 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

- (38) [6] 9 and 12, and correct algebraic work is shown.
- [5] Appropriate work is shown, but one computational or factoring error is made.
- or*
- [5] Correct work is shown to find 9, and a correct equation is written to find HJ , but no further correct work is shown.
- [4] Appropriate work is shown, but two computational or factoring errors are made.
- or*
- [4] Appropriate work is shown, but one conceptual error is made in finding JG .
- or*
- [4] Correct work is shown to find 9, but no further correct work is shown.
- [3] Appropriate work is shown, but three or more computational or factoring errors are made.
- or*
- [3] Appropriate work is shown, but one conceptual error and one computational or factoring error are made.
- or*
- [3] 9 and 12, but a method other than algebraic is used.
- [2] Appropriate work is shown, but two conceptual errors are made.
- or*
- [2] Appropriate work is shown, but one conceptual error and two or more computational or factoring errors are made.
- or*
- [2] A correct quadratic equation is written to find JG , but no further correct work is shown.
- or*

[2] Correct proportions for JG and HJ are written, but no further correct work is shown.

or

[2] An appropriate solution for the length of \overline{HJ} is found based upon an incorrectly obtained value for the length of \overline{JG} .

[1] Appropriate work is shown, but two conceptual errors and one computational or factoring error are made.

or

[1] A correct proportion for either JG or HJ is written, but no further correct work is shown.

or

[1] 9 and 12, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

Map to Core Curriculum

| Content Band | Item Numbers |
|----------------------------|---|
| Geometric Relationships | 6, 21, 23, 33 |
| Constructions | 28, 34 |
| Locus | 4, 9 |
| Informal and Formal Proofs | 2, 3, 5, 7, 8, 11, 12, 15, 16, 18, 19, 24, 25, 26, 27, 29, 31, 38 |
| Transformational Geometry | 17, 22, 30, 35 |
| Coordinate Geometry | 1, 10, 13, 14, 20, 32, 36, 37 |

Regents Examination in Geometry

January 2016

Chart for Converting Total Test Raw Scores to Final Examination Scores (Scale Scores)

The *Chart for Determining the Final Examination Score for the January 2016 Regents Examination in Geometry* will be posted on the Department's web site at: <http://www.p12.nysed.gov/assessment/> on Tuesday, January 26, 2016. Conversion charts provided for previous administrations of the Regents Examination in Geometry must NOT be used to determine students' final scores for this administration.

Online Submission of Teacher Evaluations of the Test to the Department

Suggestions and feedback from teachers provide an important contribution to the test development process. The Department provides an online evaluation form for State assessments. It contains spaces for teachers to respond to several specific questions and to make suggestions. Instructions for completing the evaluation form are as follows:

1. Go to <http://www.forms2.nysed.gov/emsc/osa/exameval/reexameval.cfm>.
2. Select the test title.
3. Complete the required demographic fields.
4. Complete each evaluation question and provide comments in the space provided.
5. Click the SUBMIT button at the bottom of the page to submit the completed form.