## FOR TEACHERS ONLY

The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

### **ALGEBRA II (Common Core)**

**Thursday,** August 18, 2016 — 12:30 to 3:30 p.m., only

#### SCORING KEY AND RATING GUIDE

#### **Mechanics of Rating**

The following procedures are to be followed for scoring student answer papers for the Regents Examination in Algebra II (Common Core). More detailed information about scoring is provided in the publication *Information Booklet for Scoring the Regents Examination in Algebra II (Common Core)*.

Do *not* attempt to correct the student's work by making insertions or changes of any kind. In scoring the constructed-response questions, use check marks to indicate student errors. Unless otherwise specified, mathematically correct variations in the answers will be allowed. Units need not be given when the wording of the questions allows such omissions.

Each student's answer paper is to be scored by a minimum of three mathematics teachers. No one teacher is to score more than approximately one-third of the constructed-response questions on a student's paper. Teachers may not score their own students' answer papers. On the student's separate answer sheet, for each question, record the number of credits earned and the teacher's assigned rater/scorer letter.

Schools are not permitted to rescore any of the open-ended questions on this exam after each question has been rated once, regardless of the final exam score. Schools are required to ensure that the raw scores have been added correctly and that the resulting scale score has been determined accurately.

Raters should record the student's scores for all questions and the total raw score on the student's separate answer sheet. Then the student's total raw score should be converted to a scale score by using the conversion chart that will be posted on the Department's web site at: <a href="http://www.p12.nysed.gov/assessment/">http://www.p12.nysed.gov/assessment/</a> by Thursday, August 18, 2016. Because scale scores corresponding to raw scores in the conversion chart may change from one administration to another, it is crucial that, for each administration, the conversion chart provided for that administration be used to determine the student's final score. The student's scale score should be entered in the box provided on the student's separate answer sheet. The scale score is the student's final examination score.

If the student's responses for the multiple-choice questions are being hand scored prior to being scanned, the scorer must be careful not to make any marks on the answer sheet except to record the scores in the designated score boxes. Marks elsewhere on the answer sheet will interfere with the accuracy of the scanning.

Part I

Allow a total of 48 credits, 2 credits for each of the following.

(1)4	(9) 1	$(17)\ldots 3\ldots$
$(2)\ldots 1\ldots$	$(10)\ldots 2\ldots .$	$(18)\ldots 3\ldots$
(3)2	$(11)\ldots 2\ldots$	$(19)\ldots 4\ldots$
(4)3	$(12)\ldots 2\ldots .$	$(20)\ldots 4\ldots$
(5) 3	$(13)\ldots 1\ldots$	$(21)\ldots 3\ldots .$
(6) 3	$(14)\ldots 1\ldots$	$(22)\ldots\ldots 4\ldots\ldots$
$(7)\ldots 1\ldots$	$(15)\ldots 3\ldots$	$(23)\ldots 2\ldots$
(8) 1	$(16)\ldots 1\ldots 1\ldots$	$(24)\ldots\ldots 4\ldots\ldots$

Updated information regarding the rating of this examination may be posted on the New York State Education Department's web site during the rating period. Check this web site at: <a href="http://www.p12.nysed.gov/assessment/">http://www.p12.nysed.gov/assessment/</a> and select the link "Scoring Information" for any recently posted information regarding this examination. This site should be checked before the rating process for this examination begins and several times throughout the Regents Examination period.

The Department is providing supplemental scoring guidance, the "Model Response Set," for the Regents Examination in Algebra II (Common Core). This guidance is recommended to be part of the scorer training. Schools are encouraged to incorporate the Model Response Sets into the scorer training or to use them as additional information during scoring. While not reflective of all scenarios, the model responses selected for the Model Response Set illustrate how less common student responses to constructed-response questions may be scored. The Model Response Set will be available on the Department's web site at <a href="http://www.nysedregents.org/algebratwo/">http://www.nysedregents.org/algebratwo/</a>.

#### **General Rules for Applying Mathematics Rubrics**

#### I. General Principles for Rating

The rubrics for the constructed-response questions on the Regents Examination in Algebra II (Common Core) are designed to provide a systematic, consistent method for awarding credit. The rubrics are not to be considered all-inclusive; it is impossible to anticipate all the different methods that students might use to solve a given problem. Each response must be rated carefully using the teacher's professional judgment and knowledge of mathematics; all calculations must be checked. The specific rubrics for each question must be applied consistently to all responses. In cases that are not specifically addressed in the rubrics, raters must follow the general rating guidelines in the publication *Information Booklet for Scoring the Regents Examination in Algebra II (Common Core)*, use their own professional judgment, confer with other mathematics teachers, and/or contact the State Education Department for guidance. During each Regents Examination administration period, rating questions may be referred directly to the Education Department. The contact numbers are sent to all schools before each administration period.

#### **II. Full-Credit Responses**

A full-credit response provides a complete and correct answer to all parts of the question. Sufficient work is shown to enable the rater to determine how the student arrived at the correct answer.

When the rubric for the full-credit response includes one or more examples of an acceptable method for solving the question (usually introduced by the phrase "such as"), it does not mean that there are no additional acceptable methods of arriving at the correct answer. Unless otherwise specified, mathematically correct alternative solutions should be awarded credit. The only exceptions are those questions that specify the type of solution that must be used; e.g., an algebraic solution or a graphic solution. A correct solution using a method other than the one specified is awarded half the credit of a correct solution using the specified method.

#### III. Appropriate Work

Full-Credit Responses: The directions in the examination booklet for all the constructed-response questions state: "Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc." The student has the responsibility of providing the correct answer **and** showing how that answer was obtained. The student must "construct" the response; the teacher should not have to search through a group of seemingly random calculations scribbled on the student paper to ascertain what method the student may have used.

Responses With Errors: Rubrics that state "Appropriate work is shown, but..." are intended to be used with solutions that show an essentially complete response to the question but contain certain types of errors, whether computational, rounding, graphing, or conceptual. If the response is incomplete; i.e., an equation is written but not solved or an equation is solved but not all of the parts of the question are answered, appropriate work has **not** been shown. Other rubrics address incomplete responses.

#### **IV.** Multiple Errors

Computational Errors, Graphing Errors, and Rounding Errors: Each of these types of errors results in a 1-credit deduction. Any combination of two of these types of errors results in a 2-credit deduction. No more than 2 credits should be deducted for such mechanical errors in a 4-credit question and no more than 3 credits should be deducted in a 6-credit question. The teacher must carefully review the student's work to determine what errors were made and what type of errors they were.

Conceptual Errors: A conceptual error involves a more serious lack of knowledge or procedure. Examples of conceptual errors include using the incorrect formula for the area of a figure, choosing the incorrect trigonometric function, or multiplying the exponents instead of adding them when multiplying terms with exponents.

If a response shows repeated occurrences of the same conceptual error, the student should not be penalized twice. If the same conceptual error is repeated in responses to other questions, credit should be deducted in each response.

For 4- and 6-credit questions, if a response shows one conceptual error and one computational, graphing, or rounding error, the teacher must award credit that takes into account both errors. Refer to the rubric for specific scoring guidelines.

#### Part II

For each question, use the specific criteria to award a maximum of 2 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

- (25) [2] Amplitude, and a correct explanation is given.
  - [1] Appropriate work is shown, but one conceptual error is made.

or

- [1] Amplitude, but the explanation is incomplete.
- [0] Amplitude, but the explanation is incorrect or missing.

or

- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (26) [2] A correct explanation is written.
  - [1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] Appropriate work is shown, but the explanation is incomplete.

or

- [1] Appropriate work is shown to demonstrate  $\left(3^{\frac{1}{5}}\right)^2 = \sqrt[5]{9}$ , but the explanation is missing or is incorrect.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (27) [2] -36xi, and correct work is shown.
  - [1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

- [1] -36xi, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (28) [2] -1.02, and correct work using the identity is shown.
  - [1] Appropriate work is shown, but one computational or rounding error is made.

[1] Appropriate work is shown, but one conceptual error is made.

or

[1] Correct work is shown to find  $\sin \theta$  but no further correct work is shown.

or

[1] -1.02, but a method other than using the identity is used.

or

- [1] -1.02, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (29) [2] Yes, and a correct justification is given, and correct work is shown.
  - [1] Appropriate work is shown, but one computational error is made.

or

[1] Appropriate work is shown, but one conceptual error is made.

or

- [1] Correct work is shown to find (150, 302), but no further correct work is shown.
- [0] Yes, but no justification is given.

or

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

(30)[2] f, and a correct justification is given. [1] Appropriate work is shown, but one computational error is made. [1] Appropriate work is shown, but one conceptual error is made. [1] Appropriate work is shown to find the x-intercept of f, but no further correct work is shown. [1] An incomplete justification is given. [0] f, but no work is shown, and no justification is written. or [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure. (31)[2] 7.5, and a correct explanation is written. [1] Appropriate work is shown, but one computational error is made. [1] Appropriate work is shown, but one conceptual error is made. [1] 7.5, but no explanation or an incorrect explanation is written. [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure. (32)[2] Independent, and correct work is shown. [1] Appropriate work is shown, but one computational error is made. [1] Appropriate work is shown, but one conceptual error is made.

or

- [1]  $P(A \cap B) = 0.3$  is found, but no further correct work is shown.
- [0] Independent, but no work is shown.

or

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

#### Part III

For each question, use the specific criteria to award a maximum of 4 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

- (33) [4] -1,  $\pm 2$ , and correct algebraic work is shown and P(x) is graphed correctly.
  - [3] Appropriate work is shown, but one computational, factoring or graphing error is made.

or

- [3] Appropriate work is shown to find two zeros and a correct graph is drawn.
- [2] Appropriate work is shown, but two or more computational, factoring, or graphing errors are made.

or

[2] Appropriate work is shown, but one conceptual error error is made.

or

[2] Appropriate work is shown to find -1 and  $\pm 2$ , but no graph is drawn.

or

- [2] A correct graph is drawn, but no further correct work is shown.
- [1] Appropriate work is shown, but one conceptual error and one computational, factoring, or graphing error are made.

or

[1] -1 and  $\pm 2$ , but a method other than algebraic is used and no graph is drawn.

- [1] -1 and  $\pm 2$ , but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (34) [4] 12, and correct work is shown.
  - [3] Appropriate work is shown, but one computational or rounding error is made.
  - [2] Appropriate work is shown, but two or more computational or rounding errors are made.

[2] Appropriate work is shown, but one conceptual error is made.

or

- [2] A correct equation, such as  $7 = 20 \left(\frac{1}{2}\right)^{\frac{t}{8.02}}$  or  $7 = 20e^{-0.0864t}$  is written, but no further correct work is shown.
- [1] Appropriate work is shown, but one conceptual error and one computational or rounding error are made.

- [1] 12, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (35) [4] 4, correct algebraic work is shown, and a correct justification and rejection are given.
  - [3] Appropriate work is shown, but one computational or factoring error is made.

- [3] 4, and appropriate work is shown, but the justification is incomplete or 8 is not rejected.
- [2] Appropriate work is shown, but two or more computational or factoring errors are made.

or

[2] Appropriate work is shown but one conceptual error is made.

or

- [2] Appropriate work is shown to find 8 and 4, but no further correct work is shown.
- [1] Appropriate work is shown, but one conceptual error and one computational or factoring error are made.

or

[1] A correct quadratic equation in standard form is written, but no further correct work is shown.

- [1] 4, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

- (36) [4] Both explanations are correctly written.
  - [3] One explanation is correct, and the other is incomplete.
  - [2] One conceptual error is made.

[2] Only one explanation is stated correctly.

- [2] Appropriate work is shown, but two partially correct explanations are written.
- [1] One incomplete explanation is written.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

#### **Part IV**

For each question, use the specific criteria to award a maximum of 6 credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

- (37) **[6]** Correct functions are written, such as  $A = 5000(1.045)^n$ ,  $B = 5000(1.0115)^{4n}$  and 67.57, 15.2, and correct work is shown.
  - [5] Appropriate work is shown, but one computational or rounding error is made.
  - [4] Appropriate work is shown, but two computational or rounding errors are made.

or

- [4] Appropriate work is shown, but one conceptual error is made.
- [3] Appropriate work is shown, but three or more computational or rounding errors are made.

or

- [3] Appropriate work is shown, but one conceptual error and one computational or rounding errors are made.
- [2] Appropriate work is shown, but one conceptual error and two or more computational errors are made.

or

[2] Appropriate work is shown, but two conceptual errors are made.

or

[2] Correct functions are written, but no further correct work is shown.

or

[2] Appropriate work is shown to find 67.57 or 15.2, but no further correct work is shown.

or

- [2] 67.57 and 15.2, but no work is shown.
- [1] Appropriate work is shown, but two conceptual errors and one computational or rounding error are made.

or

[1] Only one correct function is written.

or

[1]  $5000(1.045)^n$  and  $5000\left(1+\frac{0.046}{4}\right)^{4n}$ , but no further correct work is shown.

- [1] 67.57 or 15.2, but no work is shown.
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

# Map to the Common Core Learning Standards Algebra II (Common Core) August 2016

Question	Туре	Credits	Cluster
1	Multiple Choice	2	A-REI.B
2	Multiple Choice	2	S-IC.B
3	Multiple Choice	2	A-REI.D
4	Multiple Choice	2	S-ID.A
5	Multiple Choice	2	A-SSE.A
6	Multiple Choice	2	A-REI.D
7	Multiple Choice	2	S-CP.A
8	Multiple Choice	2	F-IF.A
9	Multiple Choice	2	A-SSE.B
10	Multiple Choice	2	F-IF.B
11	Multiple Choice	2	A-APR.D
12	Multiple Choice	2	S-IC.B
13	Multiple Choice	2	F-LE.B
14	Multiple Choice	2	F-BF.B
15	Multiple Choice	2	A-SSE.A
16	Multiple Choice	2	F-TF.A
17	Multiple Choice	2	A-REI.A
18	Multiple Choice	2	F-BF.A
19	Multiple Choice	2	G-GPE.A
20	Multiple Choice	2	A-APR.C

21	Multiple Choice	2	A-APR.B
22	Multiple Choice	2	A-SSE.B
23	Multiple Choice	2	A-REI.C
24	Multiple Choice	2	F-BF.A
25	Constructed Response	2	N-Q.A
26	Constructed Response	2	N-RN.A
27	Constructed Response	2	N-CN.A
28	Constructed Response	2	F-TF.C
29	Constructed Response	2	S-IC.B
30	Constructed Response	2	F-IF.C
31	Constructed Response	2	F-IF.B
32	Constructed Response	2	S-CP.A
33	Constructed Response	4	A-APR.B
34	Constructed Response	4	F-LE.A
35	Constructed Response	4	A-REI.A
36	Constructed Response	4	S-IC.B
37	Constructed Response	6	F-BF.A

# Regents Examination in Algebra II (Common Core) August 2016

## **Chart for Converting Total Test Raw Scores to Final Examination Scores (Scale Scores)**

The Chart for Determining the Final Examination Score for the August 2016 Regents Examination in Algebra II (Common Core) will be posted on the Department's web site at: <a href="http://www.p12.nysed.gov/assessment/">http://www.p12.nysed.gov/assessment/</a> by Thursday, August 18, 2016. Conversion charts provided for previous administrations of the Regents Examination in Algebra II (Common Core) must NOT be used to determine students' final scores for this administration.

#### Online Submission of Teacher Evaluations of the Test to the Department

Suggestions and feedback from teachers provide an important contribution to the test development process. The Department provides an online evaluation form for State assessments. It contains spaces for teachers to respond to several specific questions and to make suggestions. Instructions for completing the evaluation form are as follows:

- 1. Go to <a href="http://www.forms2.nysed.gov/emsc/osa/exameval/reexameval.cfm">http://www.forms2.nysed.gov/emsc/osa/exameval/reexameval.cfm</a>.
- 2. Select the test title.
- 3. Complete the required demographic fields.
- 4. Complete each evaluation question and provide comments in the space provided.
- 5. Click the SUBMIT button at the bottom of the page to submit the completed form.