



***New York State
Testing Program***

2022

Mathematics Test

Grade 8

Scoring Leader Materials

Training Set

Grade 8 Mathematics Reference Sheet

CONVERSIONS

1 inch = 2.54 centimeters

1 meter = 39.37 inches

1 mile = 5,280 feet

1 mile = 1,760 yards

1 mile = 1.609 kilometers

1 kilometer = 0.62 mile

1 pound = 16 ounces

1 pound = 0.454 kilogram

1 kilogram = 2.2 pounds

1 ton = 2,000 pounds

1 cup = 8 fluid ounces

1 pint = 2 cups

1 quart = 2 pints

1 gallon = 4 quarts

1 gallon = 3.785 liters

1 liter = 0.264 gallon

1 liter = 1,000 cubic centimeters

FORMULAS

Triangle

$$A = \frac{1}{2}bh$$

Parallelogram

$$A = bh$$

Circle

$$A = \pi r^2$$

Circle

$$C = \pi d \text{ or } C = 2\pi r$$

General Prisms

$$V = Bh$$

Cylinder

$$V = \pi r^2 h$$

Sphere

$$V = \frac{4}{3}\pi r^3$$

Cone

$$V = \frac{1}{3}\pi r^2 h$$

Pythagorean Theorem

$$a^2 + b^2 = c^2$$

2-Point Holistic Rubric

2 Points	<p>A 2-point response includes the correct solution to the question and demonstrates a thorough understanding of the mathematical concepts and/or procedures in the task.</p> <p>This response</p> <ul style="list-style-type: none">• indicates that the student has completed the task correctly, using mathematically sound procedures• contains sufficient work to demonstrate a thorough understanding of the mathematical concepts and/or procedures• may contain inconsequential errors that do not detract from the correct solution and the demonstration of a thorough understanding
1 Point	<p>A 1-point response demonstrates only a partial understanding of the mathematical concepts and/or procedures in the task.</p> <p>This response</p> <ul style="list-style-type: none">• correctly addresses only some elements of the task• may contain an incorrect solution but applies a mathematically appropriate process• may contain the correct solution but required work is incomplete
0 Points*	<p>A 0-point response is incorrect, irrelevant, incoherent, or contains a correct solution obtained using an obviously incorrect procedure. Although some elements may contain correct mathematical procedures, holistically they are not sufficient to demonstrate even a limited understanding of the mathematical concepts embodied in the task.</p>

* Condition Code A is applied whenever a student who is present for a test session leaves an entire constructed-response question in that session completely blank (no response attempted).

3-Point Holistic Rubric

3 Points	<p>A 3-point response includes the correct solution(s) to the question and demonstrates a thorough understanding of the mathematical concepts and/or procedures in the task.</p> <p>This response</p> <ul style="list-style-type: none"> • indicates that the student has completed the task correctly, using mathematically sound procedures • contains sufficient work to demonstrate a thorough understanding of the mathematical concepts and/or procedures • may contain inconsequential errors that do not detract from the correct solution(s) and the demonstration of a thorough understanding
2 Points	<p>A 2-point response demonstrates a partial understanding of the mathematical concepts and/or procedures in the task.</p> <p>This response</p> <ul style="list-style-type: none"> • appropriately addresses most but not all aspects of the task using mathematically sound procedures • may contain an incorrect solution but provides sound procedures, reasoning, and/or explanations • may reflect some minor misunderstanding of the underlying mathematical concepts and/or procedures
1 Point	<p>A 1-point response demonstrates only a limited understanding of the mathematical concepts and/or procedures in the task.</p> <p>This response</p> <ul style="list-style-type: none"> • may address some elements of the task correctly but reaches an inadequate solution and/or provides reasoning that is faulty or incomplete • exhibits multiple flaws related to misunderstanding of important aspects of the task, misuse of mathematical procedures, or faulty mathematical reasoning • reflects a lack of essential understanding of the underlying mathematical concepts • may contain the correct solution(s) but required work is limited
0 Points*	<p>A 0-point response is incorrect, irrelevant, incoherent, or contains a correct solution obtained using an obviously incorrect procedure. Although some elements may contain correct mathematical procedures, holistically they are not sufficient to demonstrate even a limited understanding of the mathematical concepts embodied in the task.</p>

* Condition Code A is applied whenever a student who is present for a test session leaves an entire constructed-response question in that session completely blank (no response attempted).

2022 2- and 3-Point Mathematics Scoring Policies

Below are the policies to be followed while scoring the mathematics tests for all grades:

1. If a student shows the work in other than a designated “Show your work” or “Explain” area, that work should still be scored.
2. If the question requires students to show their work, and the student shows appropriate work and clearly identifies a correct answer but fails to write that answer in the answer space, the student should still receive full credit.
3. If students are directed to show work or provide an explanation, a correct answer with **no** work shown or **no** explanation provided, receives **no** credit.
4. If students are **not** directed to show work, any work shown will **not** be scored. This applies to items that do **not** ask for any work and items that ask for work for one part and do **not** ask for work in another part.
5. If the student provides one legible response (and one response only), the rater should score the response, even if it has been crossed out.
6. If the student has written more than one response but has crossed some out, the rater should score only the response that has **not** been crossed out.
7. If the student provides more than one response, but does not indicate which response is to be considered the correct response and none have been crossed out, the student shall not receive full credit.
8. If the student makes a conceptual error (that is an error in understanding rather than an arithmetic or computational error), that student shall not receive more than 50% credit.
9. Trial-and-error responses are **not** subject to Scoring Policy #6 above, since crossing out is part of the trial-and-error process.
10. If a response shows repeated occurrences of the same conceptual error within a question, the conceptual error should **not** be considered more than once in gauging the demonstrated level of understanding.
11. In questions requiring number sentences, the number sentences must be written horizontally.
12. When measuring angles with a protractor, there is a +/- 5 degrees deviation allowed of the true measure.
13. Condition Code A is applied whenever a student who is present for a test session leaves an entire constructed-response question in that session completely blank (no response attempted). This is not to be confused with a score of zero wherein the student does respond to part or all of the question but that work results in a score of zero.

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

Answer _____ ounces

EXEMPLARY RESPONSE

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

$$\text{Rate of change} = \frac{\Delta \text{ounces}}{\Delta \text{hours}} = \frac{63 - 61\frac{1}{2}}{5 \text{ p.m.} - 2 \text{ p.m.}} = \frac{1\frac{1}{2}}{3} = \frac{1 \text{ ounce}}{2 \text{ hours}}$$

Since noon to 2 p.m. = 2 hours

$$2 \times \frac{1}{2} = 1 \text{ ounce}$$

So, the amount of oil in the lantern at 12 noon is:

$$63 + 1 = 64 \text{ ounces}$$

or other valid process

Answer 64 ounces

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

It burns at a constant rate each hour.
2 p.m: 63 ounces
5 p.m $61\frac{1}{2}$
3 hours difference
 $63 - 61.5 = 1.5$
 $1.5 \div 3 = .5$
1 p.m: 63.5 12 p.m: 64 ounces

Answer

64

ounces

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The rate of change is correctly calculated and applied to determine the correct amount of oil in the lantern at 12 noon. This response is complete and correct.

GUIDE PAPER 2

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

2pm: 63 ounces of oil
5pm: $61\frac{1}{2}$ (61.5) ounces of oil

2pm: 63 } - .5
3pm: $62\frac{1}{2}$ } - .5
4pm: 62 } - .5
5pm: $61\frac{1}{2}$ } - .5

$63 - 0.5 = 62.5$
 $62.5 - .5 = 62$
 $62 - .5 = 61.5$

constant rate: $-.5$
or
 $-\frac{1}{2}$

12pm: 64 } + .5
1pm: $63\frac{1}{2}$ } + .5
2pm: 63 } + .5

Answer 64 ounces

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The rate of change is correctly calculated and applied to determine the correct amount of oil in the lantern at 12 noon. This response is complete and correct.

GUIDE PAPER 3

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

$$\frac{63 - 61.5}{2 - 5} = \frac{1.5}{-3} = -.5$$
$$Y = ax + b$$
$$63 = -.5(2) + b$$
$$63 = -1 + b$$
$$+ 1 + 1$$
$$64 = b$$

Answer

64

ounces

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The rate of change is correctly calculated and the amount of oil in the lantern at 12 noon is correctly determined using an equation. This response is complete and correct.

GUIDE PAPER 4

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

$$\begin{aligned}63 - 61\frac{1}{2} &= 1\frac{1}{2} \\ 3 \div 1\frac{1}{2} &= .6 \\ .6 \times 2 &= 1.2 \\ 63 + 1.2 &= 64.2\end{aligned}$$

Answer

64.2

ounces

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The rate of change is miscalculated due to a calculation error. The obtained rate of change is correctly used to determine the amount of oil in the lantern at 12 noon. This response correctly addresses only some elements of the task.

GUIDE PAPER 5

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

$$\begin{pmatrix} x_1 & y_1 \\ 2 \text{ PM} & = 63 \end{pmatrix}$$

$$\begin{pmatrix} x_2 & y_2 \\ 5 \text{ PM} & = 61\frac{1}{2} \end{pmatrix}$$

↙ 12.

$$\frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{61\frac{1}{2} - 63}{5 - 2}$$

-0.5 per hour

$$\begin{array}{r} 61\frac{1}{2} \\ - 3.5 \\ \hline 58 \end{array}$$

$$\frac{-1.5}{3} = -0.5$$

Answer 58 ounces

$$\begin{array}{r} 12 \\ - 5 \\ \hline 7 \end{array}$$

$$7 \times -0.5 = -3.5$$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The rate of change is correctly calculated, but the solution is determined for 12 midnight, not 12 noon. This response correctly addresses only some elements of the task.

GUIDE PAPER 6

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

$$5-2=3$$

$$63 - 61\frac{1}{2} = 1\frac{1}{2}$$

$$1\frac{1}{2} \div 3 = \frac{3}{6}$$

$$\frac{3}{6} \times 2 = 1$$

12 to 2 hr = 2 hrs
12 to 5 hr = 3 hrs

$$12 \rightarrow 2 = 2 \text{ hrs}$$

Answer 1 ounces

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The amount of oil burned in two hours is correctly calculated, but the final step of adding this amount to the 2 p.m. total is omitted. This response correctly addresses only some elements of the task.

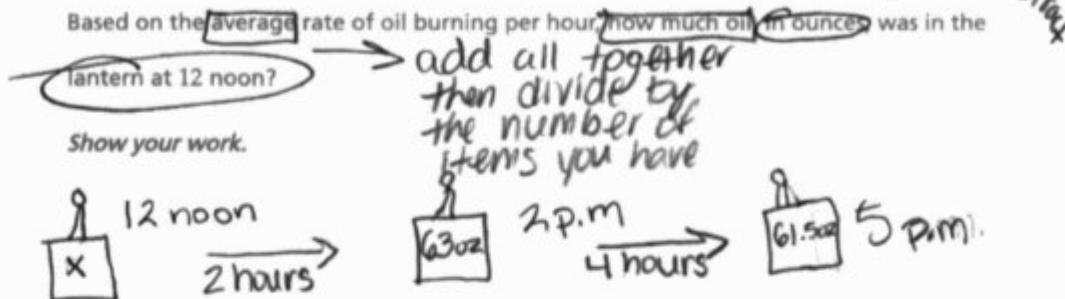
GUIDE PAPER 7

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a ~~constant rate each hour~~ ^{you can find slope} at 2 p.m. The amount of oil left in the lantern is ~~63 ounces~~ ^{63 ounces}. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. ^{Subtract}

Based on the average rate of oil burning per hour, how much oil ^{in ounces} was in the lantern at 12 noon?

Show your work.



$$4 \text{ hours} = 1.5 \text{ oz. decrease}$$

$$\frac{1.5 \text{ oz}}{4 \text{ hours}} = 0.375 \text{ oz per hour}$$

$$\begin{array}{r} 0.375 \\ \times 2 \text{ hours} \\ \hline 0.75 \text{ ounces} \end{array}$$

$$\begin{array}{r} 63 \\ - 0.75 \\ \hline 62.25 \text{ ounces} \end{array}$$

Answer 62.25 ounces

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The difference between 2 p.m. and 5 p.m. is incorrectly calculated as four hours, which causes the rate of change to be incorrect. The amount of oil burned in two hours is subtracted from the amount of oil in the lantern at 2 p.m. when it should be added.

41

A camper lights an oil lantern at 12 noon and lets it burn continuously. Once the lantern is lit, the lantern burns oil at a constant rate each hour. At 2 p.m., the amount of oil left in the lantern is 63 ounces. At 5 p.m., the amount of oil left in the lantern is $61\frac{1}{2}$ ounces. Based on the average rate of oil burning per hour, how much oil, in ounces, was in the lantern at 12 noon?

Show your work.

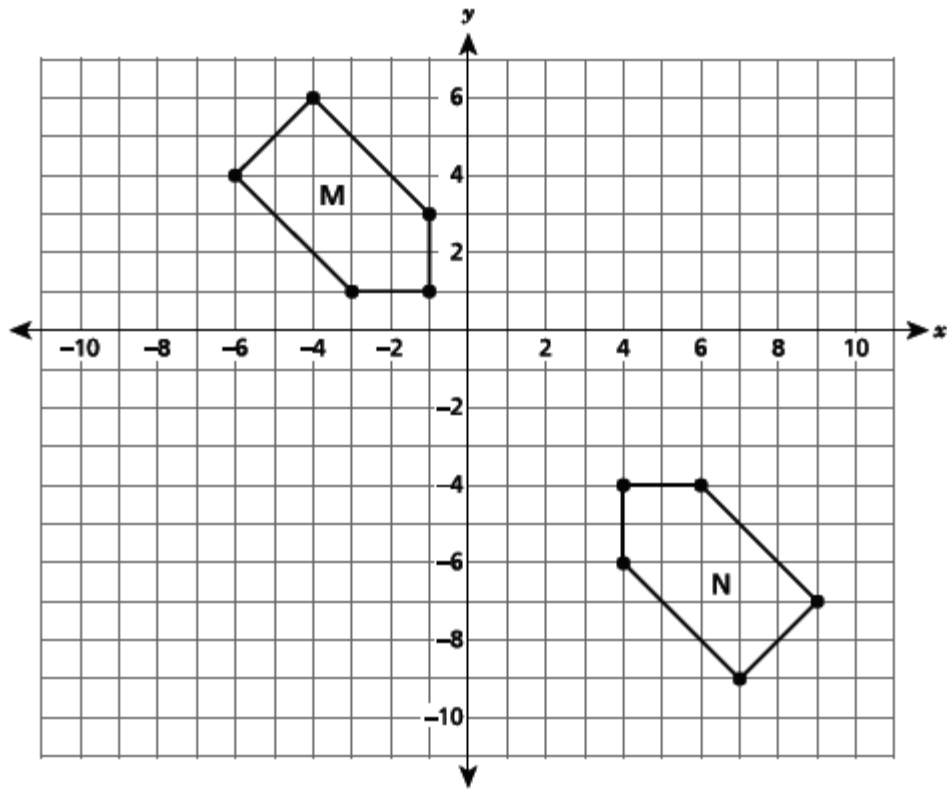
$$63 - 61\frac{1}{2} = 1\frac{1}{2}$$
$$63 + 1\frac{1}{2} = 64\frac{1}{2}$$

Answer 64 $\frac{1}{2}$ ounces

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. An incorrect procedure is used to obtain an incorrect solution.

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



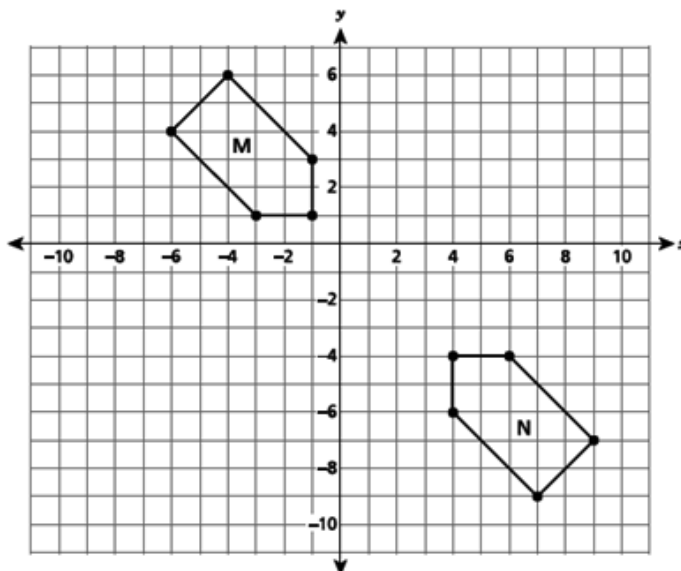
Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

EXEMPLARY RESPONSE

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

Rotate figure M clockwise or counterclockwise 180° about the origin and then translate 3 units to the right and 3 units down

or

Reflect figure M over the x -axis, reflect over the y -axis, and then translate 3 units to the right and 3 units down

or

Reflect figure M over the y -axis, reflect over the x -axis, and then translate 3 units to the right and 3 units down

or

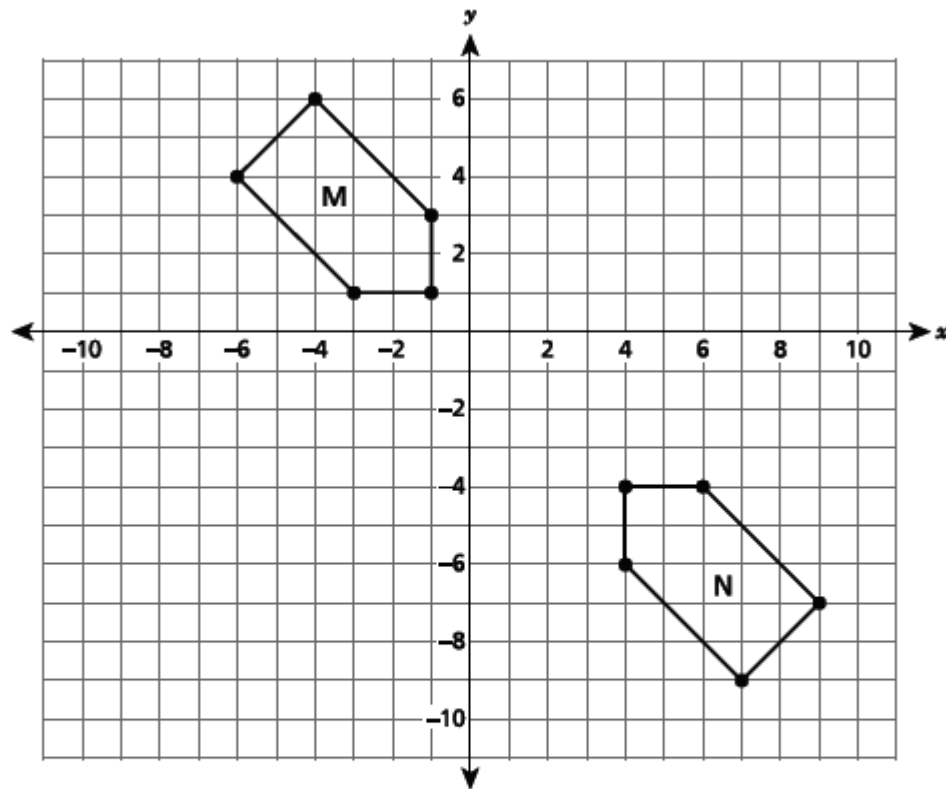
Reflect figure M over the line $y = x$, and then translate 3 units to the right and 3 units down

or

Reflect figure M over the line $y = x - 3$

or other valid process

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

First reflect over the x-axis, translate 3 units down, reflect over the y-axis, and then translate 3 units to the right.

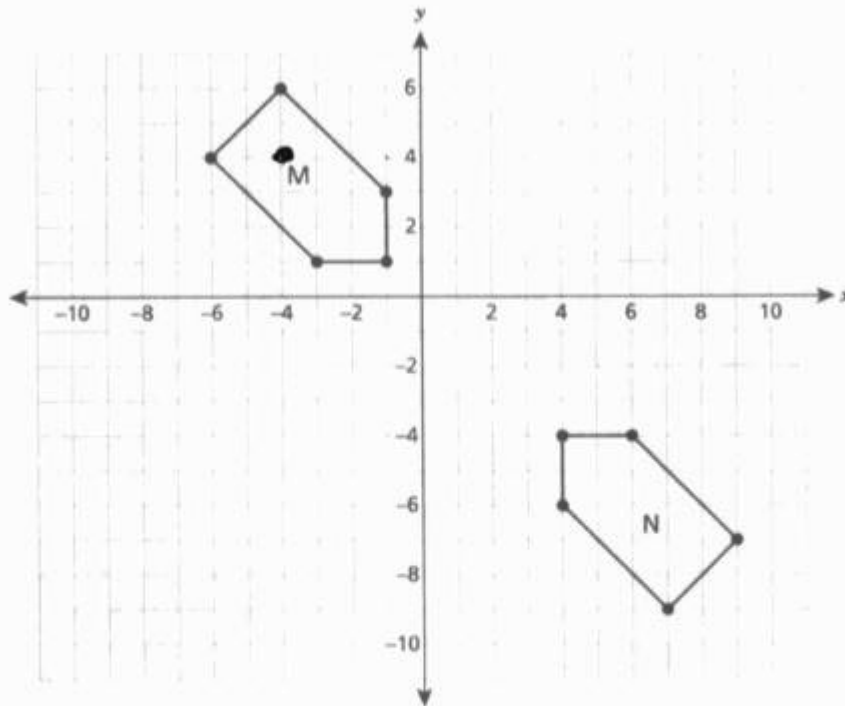
Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. A correct sequence of transformations is described to take figure M onto its congruent image, figure N. This response is complete and correct.

GUIDE PAPER 2

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

A translation of 3 units up then
3 units to the left, and a rotation of
 180°

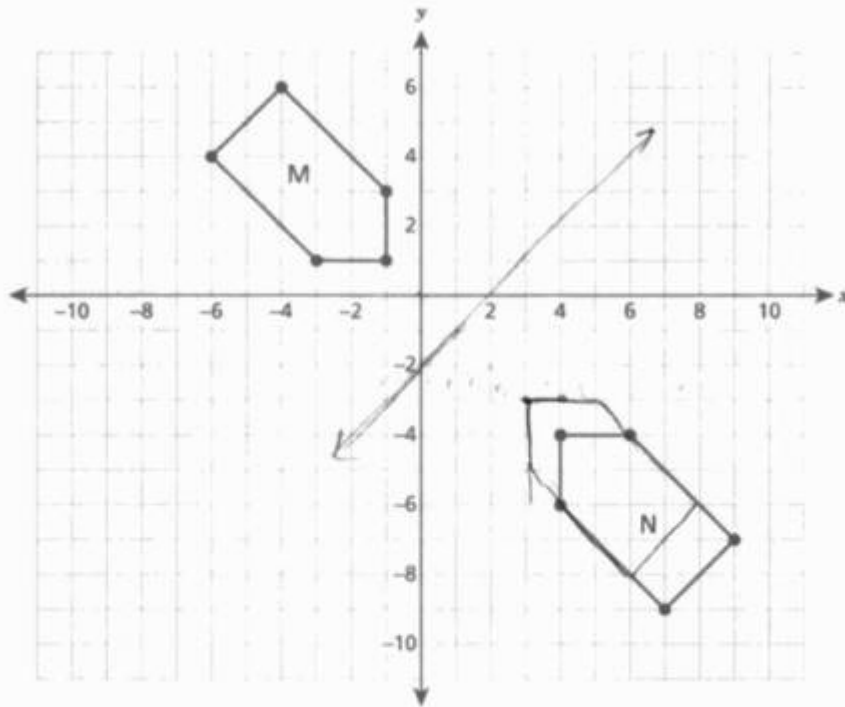
Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. A correct sequence of transformations is described to take figure M onto its congruent image, figure N.

GUIDE PAPER 3

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

~~a trans~~ A reflection of figure M over line $y = x - 2$ followed by a translation one unit down, one unit right would map figure M on top of figure N.

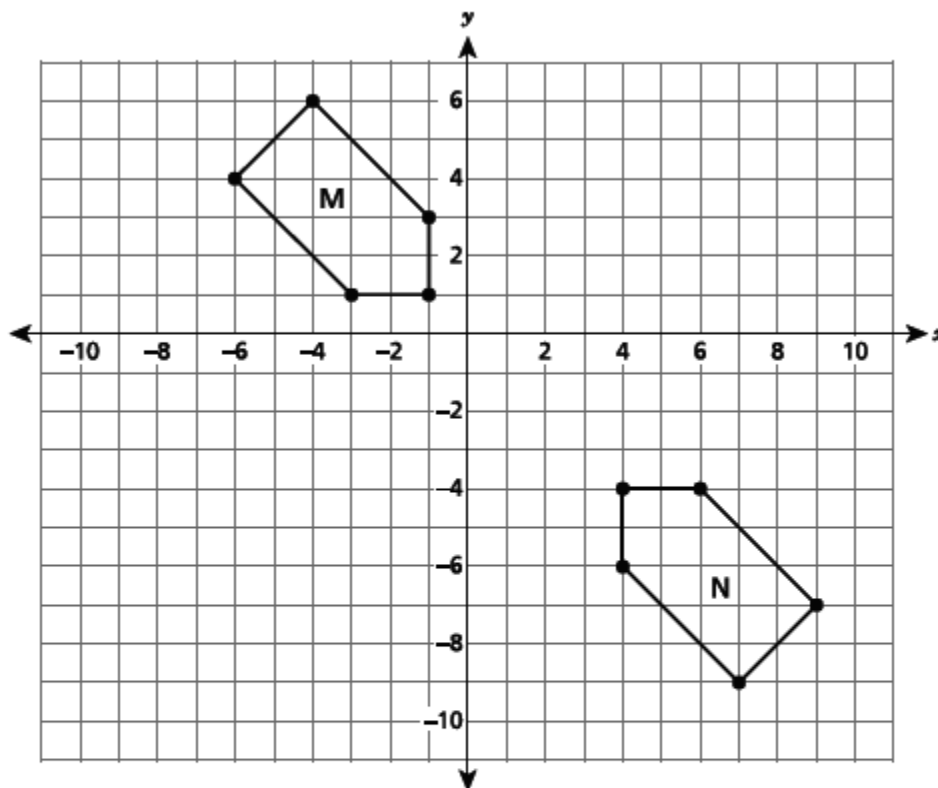
Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. A correct sequence of transformations is described to take figure M onto its congruent image, figure N.

GUIDE PAPER 4

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

M is translated three to the left and two up, then reflected across the $x=y$ line.

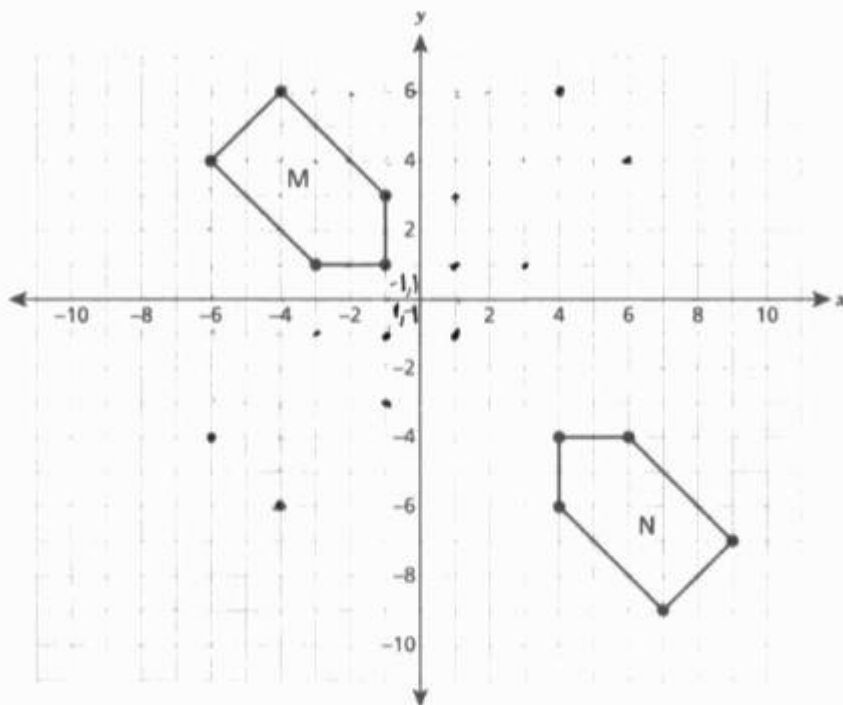
Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The reflection over the line $y = x$ is part of a correct sequence of transformations, but the translation should be three up not “two up.” This response correctly addresses only some elements of the task.

GUIDE PAPER 5

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

Reflection over Y and then a 90° rotation
clockwise.

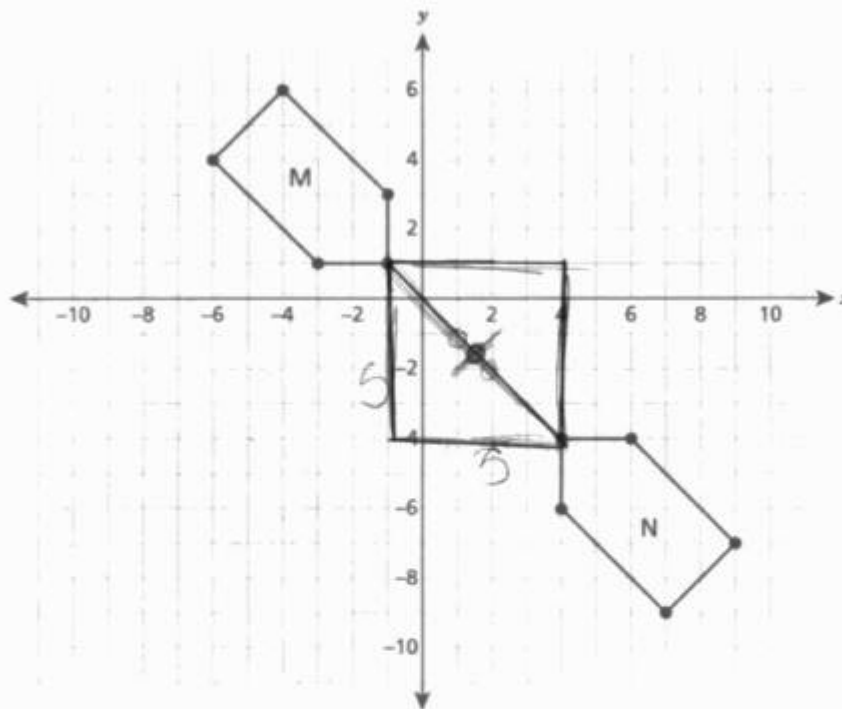
Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The reflection and rotation correctly transforms figure M into the IV quadrant in the correct orientation; however, the translation is not addressed. This response correctly addresses only some elements of the task.

GUIDE PAPER 6

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

They rotated 180° around the
point $(1.5, 1.5)$

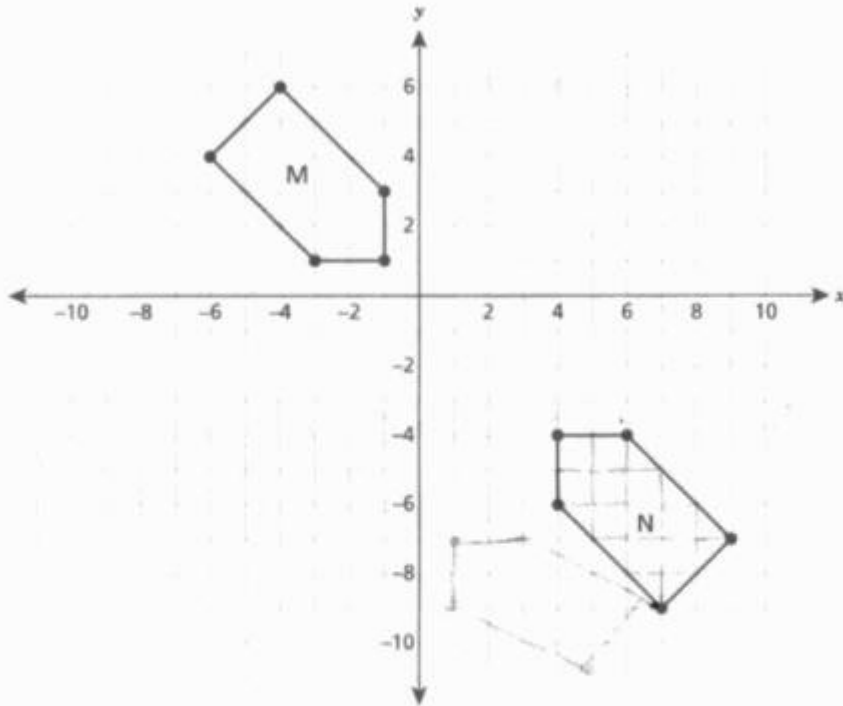
Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. Although the point of rotation is plotted correctly in the figure, an incorrect point is written in the explanation. As plotted in the figure, this transformation would be correct. This response correctly addresses only some elements of the task.

GUIDE PAPER 7

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

Explain your answer.

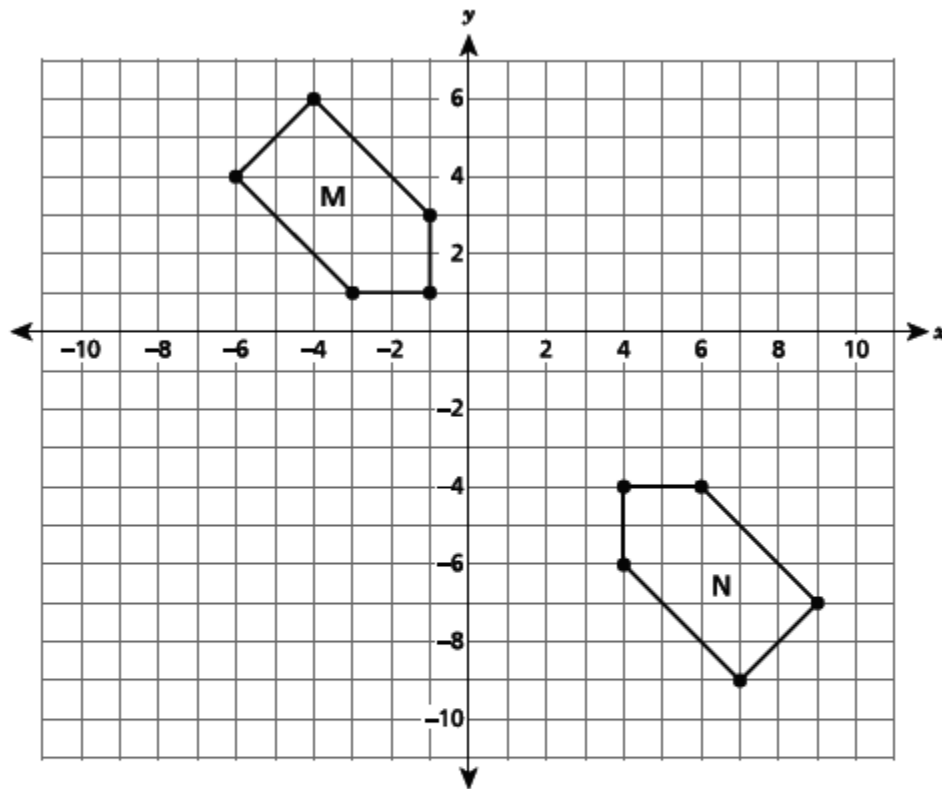
The figure flipped and rotated
which showed different points on
the graph.

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. This response is lacking any detail that could convey any understanding.

42

Figure M and its congruent image, figure N, are graphed on the coordinate plane below.



Describe a sequence of transformations that will take figure M onto its congruent image, figure N.

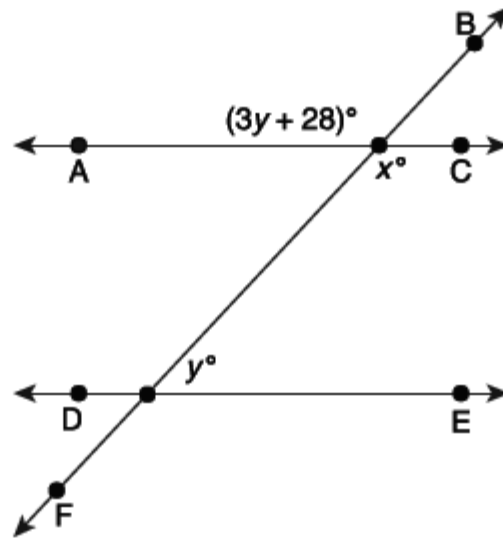
Explain your answer.

You can do a reflection over the x axis and you can move 2 units down.

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. Although the reflection over the x -axis can be part of a correct sequence of transformations, the reflection over the y -axis is ignored and an incorrect translation is described.

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

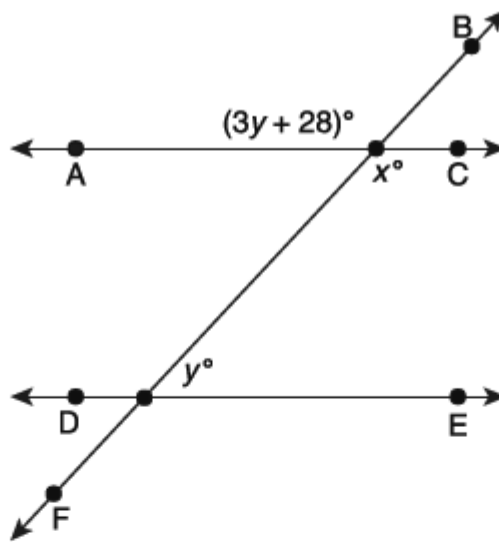
Show your work.

Answer $x =$ _____
 $y =$ _____

EXEMPLARY RESPONSE

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

Given \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} , then
the opposite angles are equivalent, and $3y + 28 = x$,
and the sum of consecutive interior angles is 180° .

$$y + (3y + 28) = 180$$

$$4y + 28 = 180$$

$$4y = 152$$

$$y = 38$$

Since the sum of supplementary angles is 180° , then

$$x + y = 180$$

$$x + 38 = 180$$

$$x = 142$$

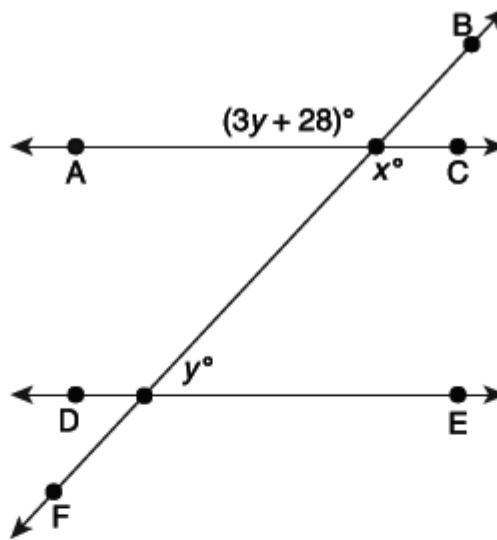
or other valid process

Answer $x = \underline{\quad 142 \quad}$

$$y = \underline{\quad 38 \quad}$$

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

$$\begin{aligned} 3y + 28 + y &= 180 \\ 4y + 28 &= 180 \\ 4y &= 152 \\ y &= 38 \end{aligned}$$

$$\begin{aligned} 38 + x &= 180 \\ x &= 142 \end{aligned}$$

Answer $x =$

$y =$

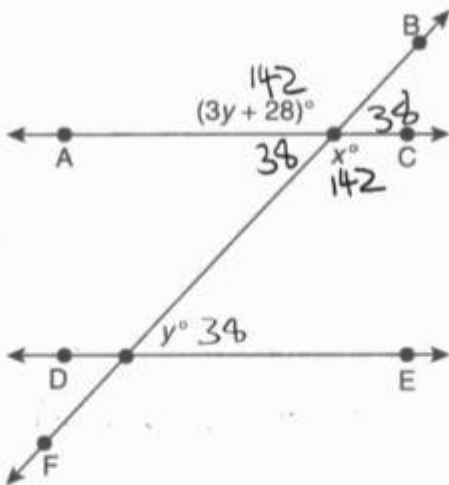
Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The solutions are solved using sound algebraic procedures and demonstrating understanding of the supplementary relationship with angles formed by parallel lines cut by a transversal. This response is complete and correct.

GUIDE PAPER 2

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



$$3(34) + 28$$

$$114 + 28$$

$$142$$

Determine the values of x and y .

Show your work.

$$3y + 28 + y = 140$$

$$4y + 28 = 140$$

$$\begin{array}{r} 4y + 28 = 140 \\ \underline{-28 \quad -28} \\ 4y = 112 \\ \underline{ } 4 } \\ y = 28 \end{array}$$

Answer $x = \underline{142}$
 $y = \underline{34}$

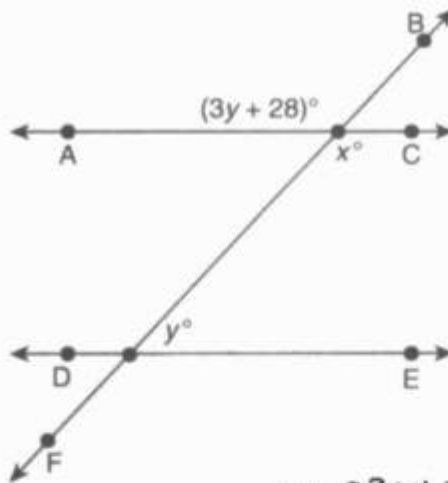
Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The solutions are solved using sound algebraic procedures and demonstrating understanding of the supplementary relationship with angles formed by parallel lines cut by a transversal. This response is complete and correct.

GUIDE PAPER 3

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

$$3y + 28 + y = 180$$

$$\begin{array}{r} 4y + 28 = 180 \\ -28 \quad -28 \\ \hline \end{array}$$

$$\frac{4y}{4} = \frac{152}{4}$$

$$y = 38$$

$$180 - 38 = 142$$

$$x = 142$$

$$\text{Answer } \begin{array}{l} x = \underline{142} \\ y = \underline{38} \end{array}$$

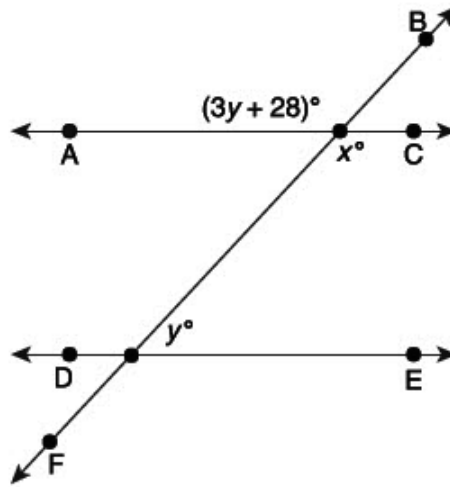
Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The solutions are solved using sound algebraic procedures and demonstrating understanding of the supplementary relationship with angles formed by parallel lines cut by a transversal. This response is complete and correct.

GUIDE PAPER 4

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

$$(3y + 28) + y = 180$$

$$(3y + 28) + y = 180$$

$$4y + 28 = 180$$

$$\begin{array}{r} 4y + 28 = 180 \\ -28 \quad -28 \\ \hline 4y = 152 \end{array} \quad x = 152$$

$$4y = 152 \rightarrow y = 38$$

Answer $x =$

$y =$

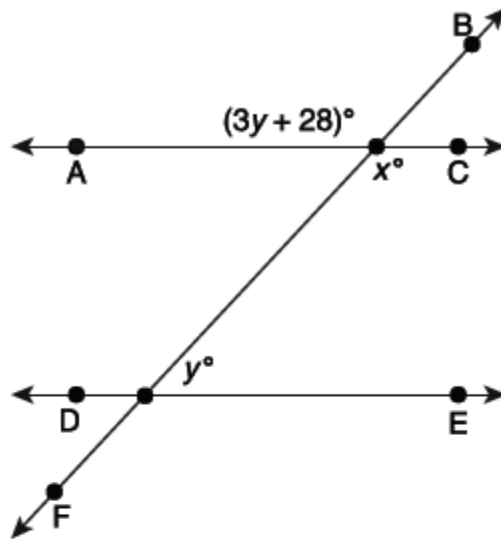
Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The process to solve for y is correct, and the y solution is correct. No work is shown for x , so it is unclear how the incorrect value of x is calculated. This response correctly addresses only some elements of the task.

GUIDE PAPER 5

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

$$\begin{aligned} X &= 3y + 28 \\ D &= y \\ 3y + 28 + y &= 180 \\ 4y + 28 &= 180 \\ 4y &= 152 \\ Y &= 38 \\ 3(38) + 28 &= x \\ 76 + 28 &= x \\ X &= 104 \end{aligned}$$

Answer $x =$

$y =$

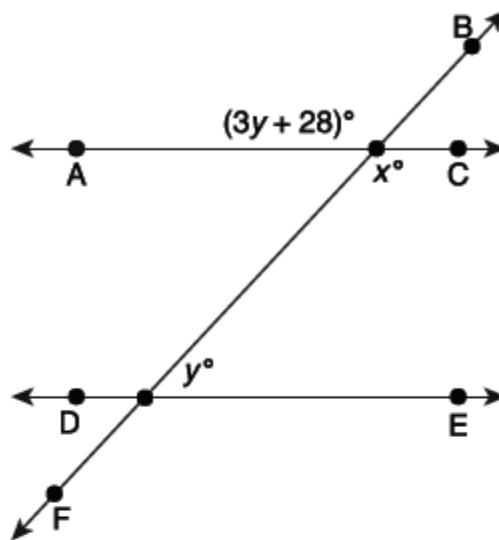
Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The value of y is correctly calculated using a sound procedure. A calculation error ($3 \times 38 \neq 76$) results in an incorrect value of x . This response correctly addresses only some elements of the task.

GUIDE PAPER 6

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

$$\begin{aligned} 3y+28+y &= 180 \\ 4y+28 &= 180 \\ -28 \quad -28 & \\ 4y &= 152/4 \\ y &= 38 \end{aligned}$$

$$\begin{aligned} 3y+28+x &= 180 \\ 3(38)+28+x &= 180 \\ 114+28+x &= 180 \\ 142+x &= 180 \\ -142 \quad -142 & \end{aligned}$$

Answer $x =$ $x=38$

$y =$ $y=38$

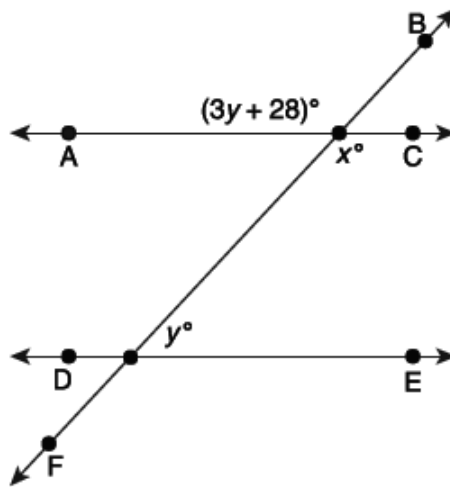
Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The value of y is correctly calculated using a sound procedure. The equation used to solve for x is incorrect. This response correctly addresses only some elements of the task.

GUIDE PAPER 7

43

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

$$\begin{aligned} &(3y + 28 \text{ degrees}) \\ &y = 43 \text{ degrees} \\ &3(43 \text{ degrees}) + 28 \text{ degrees} \\ &= 157 \\ &x = 136 \end{aligned}$$

Answer $x =$

43 degrees
I found this by
using the
protractor that
was given at the
beginning of
the test.

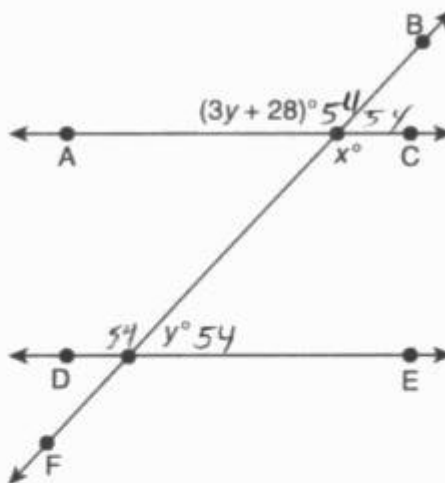
$y =$

157 degrees
I found this by
using the
protractor that
was given at the
beginning of
the test.

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. An incorrect procedure is used to determine an incorrect solution.

In the figure shown below, \overleftrightarrow{AC} is parallel to \overleftrightarrow{DE} with transversal \overleftrightarrow{BF} .



Determine the values of x and y .

Show your work.

$$\begin{array}{r}
 3y + 28 = 180 \\
 - 28 \quad - 28 \\
 \hline
 3y = 162 \\
 \frac{3y}{3} = \frac{162}{3} \\
 y = 54
 \end{array}$$

$$\begin{array}{r}
 54 \\
 54 \\
 108 \\
 180 \\
 \hline
 72 \\
 54
 \end{array}$$

Answer $x = \underline{72}$
 $y = \underline{54}$

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. An incorrect equation is used to solve for the value of y . An error occurs when subtracting 28 ($180 - 28 \neq 162$). The calculated values of x and y do not sum to 180, which shows a lack of understanding of supplementary angles.

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

Step 1: $-6x + 15 = 8x + 24$

Step 2: $15 = 2x + 24$

Step 3: $-9 = 2x$

Step 4: $x = -\frac{9}{2}$

What error did the student make and what is the correct value of x ?

Explain your answer.

Answer $x =$ _____

EXEMPLARY RESPONSE

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

$$\text{Step 1: } -6x + 15 = 8x + 24$$

$$\text{Step 2: } 15 = 2x + 24$$

$$\text{Step 3: } -9 = 2x$$

$$\text{Step 4: } x = -\frac{9}{2}$$

What error did the student make and what is the correct value of x ?

Explain your answer.

An error is made in Step 2 when $-6x$ is added to $8x$ to get $2x$, but $6x$ should be added to $8x$ get $14x$. The value of x is $-\frac{9}{14}$.

or other valid explanation

Answer $x = \underline{\quad -\frac{9}{14} \quad}$

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

Step 1: $-6x + 15 = 8x + 24$

Step 2: $15 = 2x + 24$

Step 3: $-9 = 2x$

Step 4: $x = -\frac{9}{2}$

$$\begin{array}{r} 15 = 14x + 24 \\ -24 \quad -24 \\ \hline -9 = 14x \\ \frac{-9}{14} = \frac{14x}{14} \quad x = \end{array}$$

What error did the student make and what is the correct value of x ?

Explain your answer.

The student subtracted $6x$ from $8x$ when they were supposed to add $6x$ to $8x$.

Answer $x = \frac{-9}{14}$

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The error is correctly explained. The correct value of x is provided. This response is complete and correct.

GUIDE PAPER 2

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

Step 1: $-6x + 15 = 8x + 24$

Step 2: $15 = 2x + 24$

Step 3: $-9 = 2x$

Step 4: $x = -\frac{9}{2}$

What error did the student make and what is the correct value of x ?

Explain your answer.

The student made an error in step 1-2. the student did $8x-6x$ instead of $8x+6x$. They end up etting $2x$ which is wrong.

Answer $x =$

$$\frac{-9}{14}$$

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The error is correctly explained. The correct value of x is provided. This response is complete and correct.

GUIDE PAPER 3

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

Step 1: $-6x + 15 = 8x + 24$

Step 2: $15 = 2x + 24$

Step 3: $-9 = 2x$

Step 4: $x = -\frac{9}{2}$

What error did the student make and what is the correct value of x ?

Explain your answer.

Step 1 is correct but when he got to step 2 and subtracted the $6x$ to $8x$ but you are supposed to add it because you have to change the symbol.

Answer $x =$

$$-6x + 15 = 8x + 24$$

$$15 = 14x + 24$$

$$-9 = 14x$$

$$-\frac{9}{14}$$

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The error is correctly explained. The correct value of x is provided. This response is complete and correct.

GUIDE PAPER 4

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

$$\text{Step 1: } -6x + 15 = 8x + 24$$

$$\text{Step 2: } 15 = 2x + 24$$

$$\text{Step 3: } -9 = 2x$$

$$\text{Step 4: } x = -\frac{9}{2}$$

What error did the student make and what is the correct value of x ?

Explain your answer.

The student didn't do the opposite operation when adding. Instead of doing $6x + 8x$ he didn't change change the negative sign, and he did $-6x + 8x$.

$$-6 + (-8)$$

$$15 = 14x + 24$$

$$-14x = 9$$

$$-9 = 14x$$

Answer $x = \underline{-0.64}$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The error is correctly explained; however, the value of x is incorrect as it is rounded or truncated. This response correctly addresses only some elements of the task.

GUIDE PAPER 5

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

Step 1: $-6x + 15 = 8x + 24$

Step 2: $15 = 2x + 24$

Step 3: $-9 = 2x$

Step 4: $x = -\frac{9}{2}$

What error did the student make and what is the correct value of x ?

Explain your answer.

they subtracted $-6x$ instead of adding it to balance out the equation.

Answer $x =$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The value of x is correct. The explanation correctly identifies the location of the mistake; however, an incorrect sign is used: the error should be described as adding $-6x$, or subtracting $6x$. This response correctly addresses only some elements of the task.

GUIDE PAPER 6

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

$$\text{Step 1: } -6x + 15 = 8x + 24$$

$$\text{Step 2: } 15 = 2x + 24$$

$$\text{Step 3: } -9 = 2x$$

$$\text{Step 4: } x = -\frac{9}{2}$$

What error did the student make and what is the correct value of x ?

Explain your answer.

The student didn't combined like terms correctly.

Answer $x =$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The value of x is correct. The explanation is incomplete: it is unclear which terms are being incorrectly combined. This response correctly addresses only some elements of the task.

GUIDE PAPER 7

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

$$\text{Step 1: } -6x + 15 = 8x + 24 \rightarrow 39$$

$$\text{Step 2: } 15 = 2x + 24$$

$$\text{Step 3: } -9 = 2x \quad \frac{39}{2} = \frac{2x}{2}$$

$$\text{Step 4: } x = -\frac{9}{2} \quad x = 19.5$$

What error did the student make and what is the correct value of x ?

Explain your answer.

The student subtracted $15 - 24$ instead of adding it.
which gave you 39 then you had to divide
it by 2 .

Answer $x = 19.5$

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The error is incorrectly identified and explained. The value of x is incorrectly determined. Holistically, no understanding is shown.

44

The steps a student took to solve an equation are shown below.

$$\frac{3}{4}(-8x + 20) = -8(-x - 3)$$

Step 1: $-6x + 15 = 8x + 24$

Step 2: $15 = 2x + 24$

Step 3: $-9 = 2x$

Step 4: $x = -\frac{9}{2}$

What error did the student make and what is the correct value of x ?

Explain your answer.

in step 3 the student didnt get rid of the coefficient

Answer

$x =$

-4.5

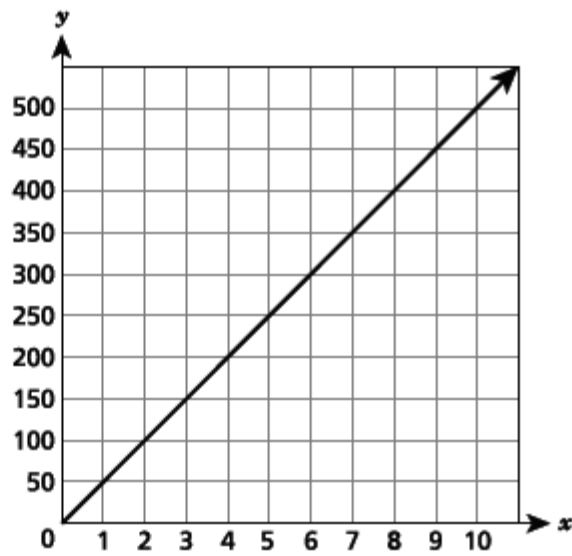
Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The explanation of the error is incorrect. A decimal equivalent of $-\frac{9}{2}$ is provided as the solution.

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B

What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

EXEMPLARY RESPONSE

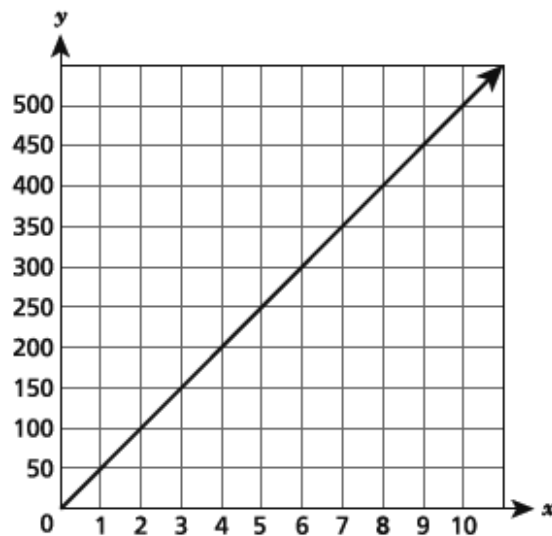
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

Function A has a rate of change of 35, represented by the slope of the given equation.

The line for Function B passes through the points (1, 50), (2, 100), (3, 150), etc. So, the slope is $50 \div 1$ or a rate of change of 50.

The difference in the rates of change between the two functions is:

$50 - 35 = 15$ or Function B has a rate of change that is 15 units greater than Function A

or

$35 - 50 = -15$ or Function A has a rate of change that is 15 units less than Function B

or other valid explanation

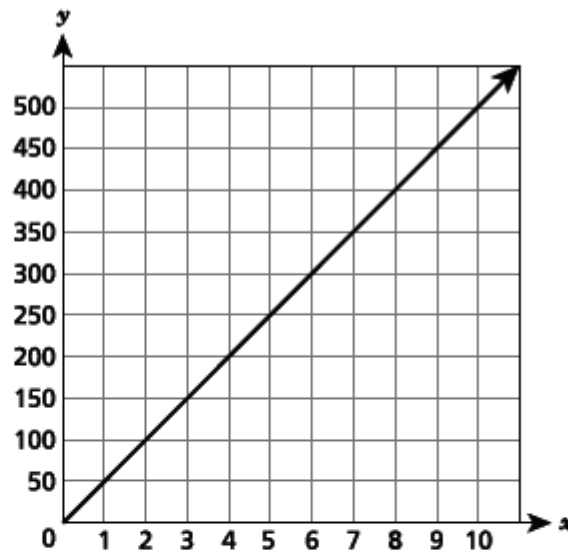
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

function a	function b	$50 - 35 = 15$
$y = 35x$	$m = \frac{\text{rise}}{\text{run}} = \frac{50}{1} = 50$	
$m = 35$	$m = 50$	

The difference in rate of change is 15. The rate of change for function b is 50 and the rate of change for function a is 35, and when you subtract 35 from 50, you get a difference of 15.

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The rates of change are correctly determined for both functions. The difference in the rates of change between the functions is correctly explained. This response is complete and correct.

GUIDE PAPER 2

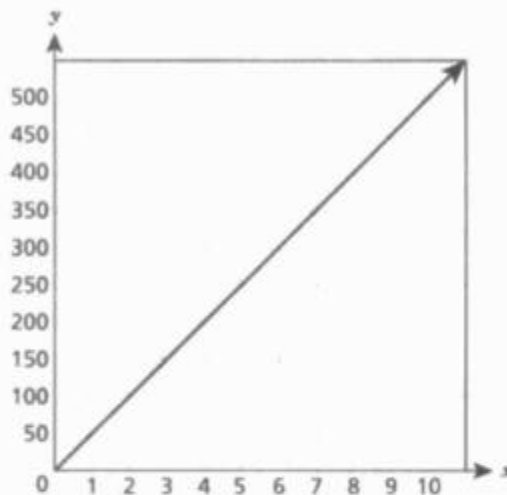
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

The difference in the rate of change between Function A and Function B is -15. This is because the rate of change in Function A is 35 and the rate of change in Function B is 50. $35 - 50 = -15$

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The rates of change are correctly determined for both functions. The difference in the rates of change between the functions is correctly explained. This response is complete and correct.

GUIDE PAPER 3

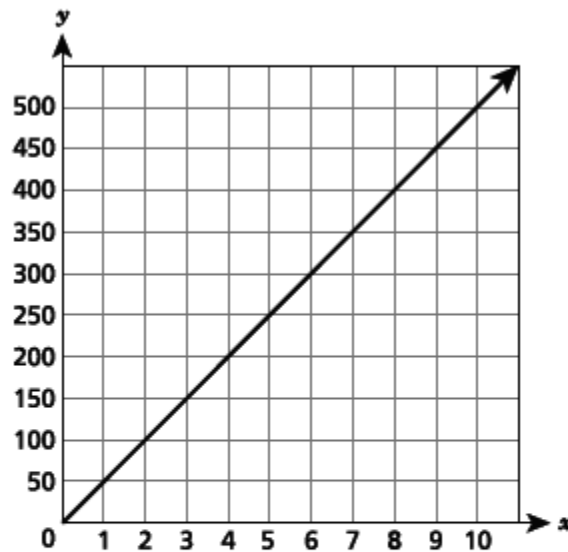
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

The difference is 15 because the rate of change for function A is 35 and function B is 50, and $50 - 35 = 15$.

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The rates of change are correctly determined for both functions. The difference in the rates of change between the functions is correctly explained. This response is complete and correct.

GUIDE PAPER 4

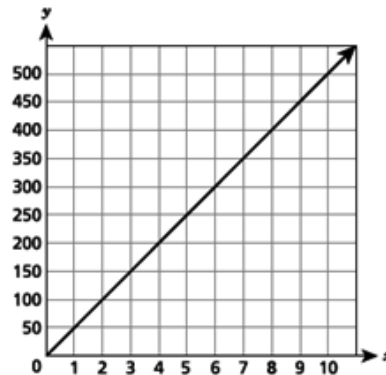
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

$$m = \frac{\Delta y}{\Delta x}$$
$$m = \frac{150 - 100}{3 - 2}$$
$$m = \frac{50}{1}$$
$$m = 50$$

$$y = mx + b$$
$$100 = 50(2) + b$$
$$100 = 100 + b$$
$$-100 \quad -100$$

$$0 = b$$

$$y = 50x$$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. A correct equation is written for Function B, and the rate of change is correctly identified and defined for this function; however, the rate of change for Function A and the difference in the rates of change between the functions are not addressed. This response correctly addresses only some elements of the task.

GUIDE PAPER 5

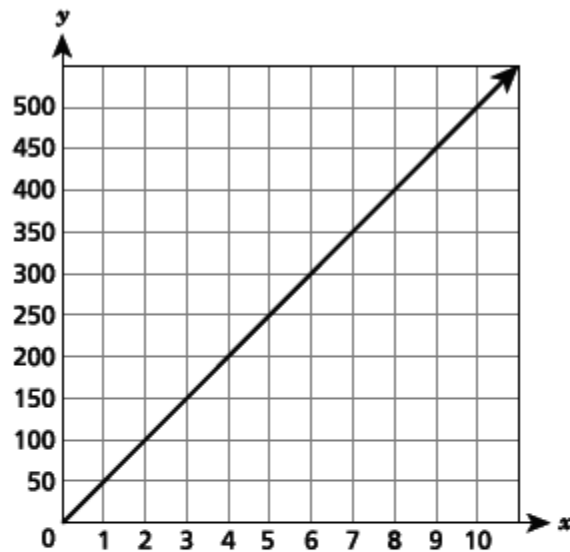
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

function b goes $y = \frac{50}{1} x$

function a goes $y = \frac{35}{1} x$

meaning function B is a faster rate of change

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The rates of change of both functions are correctly identified, but the difference in the rates of change between the functions is not calculated. This response correctly identifies only some elements of the task.

GUIDE PAPER 6

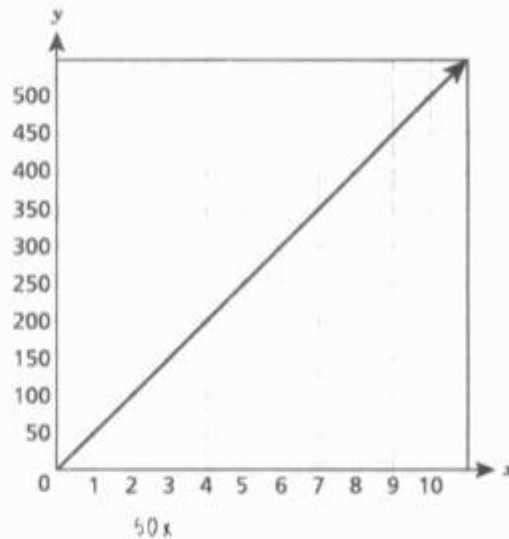
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

The difference in rates of change in function A and B is $15x$. Since function A has a rate of change of $35x$, and function B has a rate of change of $50x$, subtracting the two constant rates gives a difference of $15x$.

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The value of the coefficients represents correct rates of change; however, attaching the variable x is not correct. Again, the value of the coefficient represents the difference in the rates of change between the functions; however, attaching the variable x is not correct. This response correctly addresses only some elements of the task.

GUIDE PAPER 7

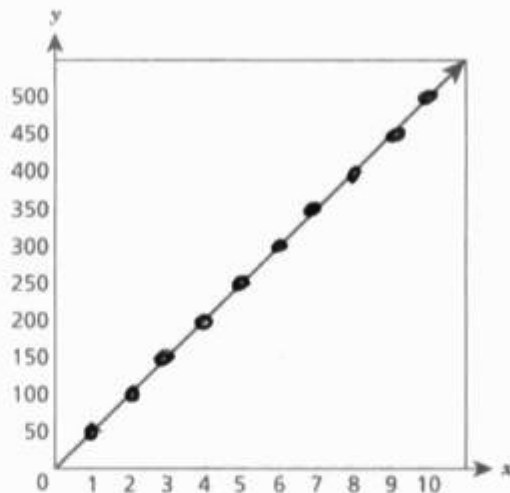
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

Function b will stay constant because it keep increasing by 50. function A doesn't stay constant

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. Although the response contains the correct rate of 50 for Function B, the explanation is contradictory. The difference in the rates of change between the functions is not calculated.

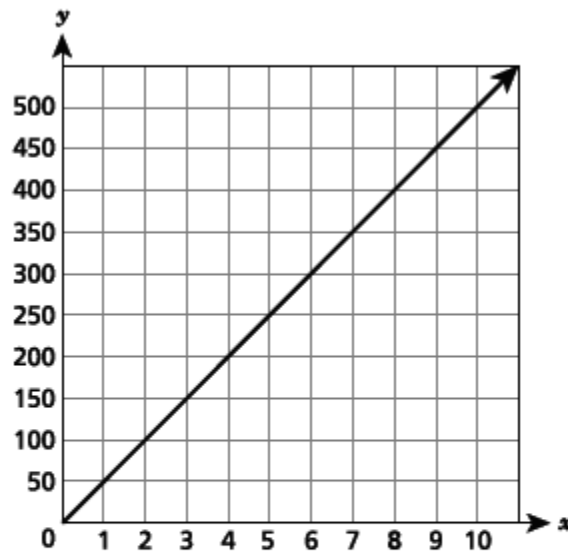
45

Two functions are represented below.

FUNCTION A

$$y = 35x$$

FUNCTION B



What is the difference in the rate of change between Function A and Function B? Be sure to include the rate of change of each function in your answer.

Explain your answer.

the rate of change for a is 35 while b is 2 so the difference is 32.

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The rate of change for B is incorrect, and the difference between the provided rate of change of Function A and that of Function B is incorrectly calculated.

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

Answer _____ gallons

EXEMPLARY RESPONSE

46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$V = \pi r^2 h$$

$$r = \frac{1}{2}d, \text{ so } r = \frac{1}{2}(12) = 6 \text{ inches}$$

$$V = \pi 6^2(10) = 360\pi \text{ cubic inches or } 1131 \text{ cubic inches}$$

(While using a value such as 1131 in place of 360π is the result of early rounding, in that the full value displayed on the calculator is very cumbersome and unwieldy, it is acceptable in this instance to use the rounded value because this does not detract from demonstrating a full understanding.)

To convert to gallons, divide by 231, so

$$V = 360\pi \div 231 \approx 4.8959 \text{ gallons}$$

Then round to the nearest gallon, which is 5.

or other valid process

Answer 5 gallons

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

The container has a height of 10 inches and a diameter of 12 inches.

• There are 231 cubic inches in one gallon of sand. $\frac{12}{2} = 6$

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$V = \pi r^2 \cdot h$$

$$\pi (6)^2 \cdot 10$$

$$\pi 36 \cdot 10$$

$$360\pi$$

$$1130.97$$

$$\begin{array}{r} \text{xxx } 4.89597 \\ 231 \overline{) 1130.97} \\ \underline{924} \\ 206.97 \end{array}$$

Answer 5 gallons

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The volume of the sand is correctly calculated and rounded to the nearest gallon to determine the correct solution. This response is complete and correct.

GUIDE PAPER 2

46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$V = \pi r^2 h$$

$$V = \pi \cdot 6^2 \cdot 10$$

$$V = 1130.97$$

$$23 \overline{)1130.97} \quad 4.89$$

Answer 5 gallons

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The volume of the sand is correctly calculated and rounded to the nearest gallon to determine the correct solution. This response is complete and correct.

GUIDE PAPER 3

46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$V = \pi \times r^2 \times h$$

$$V = \pi \times 6^2 \times 10$$

$$V = 360\pi \text{ inches}^3$$

$$360\pi \text{ inches}^3 \div 231 \text{ inches}^3 / \text{gallon}$$

$$= \text{approximately } 5 \text{ gallons}$$

Answer

5

gallons

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The volume of the sand is correctly calculated and rounded to the nearest gallon to determine the correct solution. This response is complete and correct.

GUIDE PAPER 4

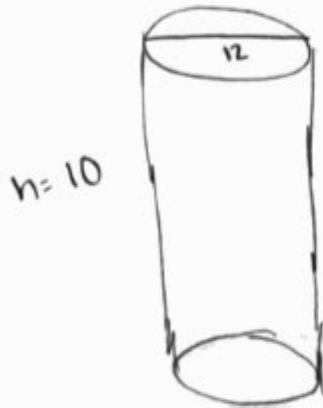
46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.



$$\begin{aligned} V &= \pi r^2 h \\ V &= \pi 6^2 10 \\ \pi 36 &= 10 \\ \pi &= 360 \\ \frac{1130.97}{231} &= 4.89 \end{aligned}$$

Answer 4 gallons

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The volume of the sand is correctly calculated. The conversion to gallons uses the correct process, but the solution is not rounded to the nearest gallon. This response correctly addresses only some elements of the task.

GUIDE PAPER 5

46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$12/2=6^2=36*10=360/231 \text{ 1.558... about 2}$$

Answer

About 2

gallons

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The value of π is omitted while computing the volume of the sand. A correct process is used to convert to gallons, and the provided solution is rounded to the nearest gallon. This response correctly addresses only some elements of the task.

GUIDE PAPER 6

46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$\begin{aligned}V &= \pi r \times r \times h \\V &= \pi \times 6 \times 6 \times 10 \\V &= \pi \times 360 \\V &= 1131\end{aligned}$$

Answer

v=1131

gallons

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The volume of the sand is correctly calculated, but the conversion to gallons is not addressed. This response correctly addresses only some elements of the task.

GUIDE PAPER 7

46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$V = \pi r^2 h$$

$$V = \pi 12^2 10 = 1440$$

$$1440 \div 231 = 6.23 = 6$$

Answer 6 gallons

Score Point 0 (out of 2 points)

Although the provided solution is correctly converted to the nearest gallon, holistically, this response is not sufficient to demonstrate even a limited understanding of the mathematical concepts embodied in the task. The diameter is used for the radius in the equation. While calculating the volume, π is written in the equation, but ignored in the work.

46

At the beach, a child uses a container in the shape of a cylinder to build a sand castle. The child completely fills the container with sand.

- The container has a height of 10 inches and a diameter of 12 inches.
- There are 231 cubic inches in one gallon of sand.

What is the approximate volume of sand, in gallons, in the container? Round your answer to the nearest gallon.

Show your work.

$$V = \pi r^2 h$$

$$V = \pi 24^2 10$$

$$V = 5760\pi$$

Answer

$$V = 5760\pi$$

gallons

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. Double the value of the diameter is used for the radius in the volume equation, which is a conceptual error. The volume of the sand is not converted to gallons.

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

Answer $x =$ _____

EXEMPLARY RESPONSE

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

$$3.2 - \frac{1}{2}x - 2 = 4.8x + 2 - 5.2x$$

$$1.2 - \frac{1}{2}x = 2 - 0.4x$$

$$-0.8 - \frac{1}{2}x = -0.4x$$

$$-0.8 = 0.1x$$

$$x = -8$$

or other valid process

Answer $x = \underline{\quad -8 \quad}$

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$\textcircled{3.2} - \frac{1}{2}x \textcircled{-2} = \boxed{4.8x} + 2 \textcircled{-5.2x}$$

$$\begin{array}{r} 1.2 - \cancel{.5x} \\ \hline -2.00 + \cancel{.5x} \\ \hline -0.8 \end{array} = \begin{array}{r} -.4x + 2 \\ \hline +.5x - \cancel{2} \\ \hline -.1x + 2 \end{array}$$

$$\frac{-0.8}{.1} = \frac{-.1x + 2}{.1}$$

$$\boxed{x = -8}$$

(K)

$$3.2 - \frac{1}{2}(-8 + 4) = 4.8(-8) + 2 - 5.2(-8)$$

$$3.2 - \frac{1}{2}(-4) = -38.4 + 2 + 41.6$$

$$3.2 + 2 = 5.2$$

$$5.2 = 5.2 \checkmark$$

Answer $x = \underline{-8}$

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The equation is solved correctly using mathematically sound procedures. Although not required, the solution is checked. This response is complete and correct.

GUIDE PAPER 2

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$3.2 - \frac{1}{2}(x+4) = 4.8x + 2 - 5.2x$$

$$3.2 - \frac{1}{2}x - 2 = 4.8x + 2 - 5.2x$$

$$3.2 - 2 = 5.3x + 2 - 5.2x$$

$$1.2 = 0.1x + 2$$

$$-0.8 = 0.1x$$

$$x = -8$$

Answer $x =$

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The equation is solved correctly using mathematically sound procedures. This response is complete and correct.

GUIDE PAPER 3

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$\begin{aligned} 3.2 - 1/2x - 2 - 2 &= -0.4x \\ -0.8 &= 0.1x \\ .1x &= -0.8 \\ x &= -8 \end{aligned}$$

Answer $x =$

Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. The equation is solved correctly using mathematically sound procedures. The amount of work shown is sufficient for full credit. This response is complete and correct.

GUIDE PAPER 4

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$1.2 - 1/2 x = -0.4 x + 2$$

-8

Answer $x =$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. Although the equation is solved correctly, the work to show how the solution is obtained is limited.

GUIDE PAPER 5

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

$$3.2 - 0.5x - 2 = -0.4x + 2$$

$$1.2 - 0.5x = -0.4x + 2$$

$$+0.4x \quad -0.4x$$

$$1.2 - 0.1x = 2$$

$$-1.2 \quad -1.2$$

$$-0.1x = 0.8$$

$$\div \quad -0.1$$

$$x = 8$$

Answer $x = 8$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. The distribution property is used correctly, and the like terms are combined correctly, but a sign error occurs in the final step. This response contains an incorrect solution but applies a mathematically appropriate process.

GUIDE PAPER 6

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$3.2 - \frac{1}{2}x + 2 = -0.4x + 2$$

$$5.2 - \frac{1}{2}x = -0.4x + 2$$

$$5.2 = 0.1x + 2$$

$$3.2 = 0.1x$$

$$x = 32$$

Answer $x =$

Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts and procedures in the task. An error is made when distributing ($-\frac{1}{2} \times 4 \neq 2$). The rest of the work is correct. This response correctly addresses only some elements of the task.

GUIDE PAPER 7

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$\begin{aligned} 3.2 - 1/2(x+4) &= 4.8x + 2 - 5.2x \\ 3.2 - 1/2 + 4x &= 4.8x + 2 - 5.2x \\ 3.2 - 1/2 + 4x &= -0.4x + 2 \\ 3.2 - 1/2 &= -4.4x + 2 \\ 1.2 - 1/2 &= -4.4x \\ 0.7 &= -4.4x \\ x &= -6.285714286... \end{aligned}$$

Answer $x =$

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. A distribution error occurs ($-\frac{1}{2}(x + 4) \neq -\frac{1}{2} + 4x$). The final solution is incorrectly obtained with an inverted division ($x = -0.7/4.4$, not $x = -4.4/0.7$). Holistically, this response shows no overall understanding of how to solve this equation.

47

Determine the solution to the equation shown below.

$$3.2 - \frac{1}{2}(x + 4) = 4.8x + 2 - 5.2x$$

Show your work.

$$\begin{aligned} 3.2 - 0.5(x + 4) &= 4.8x + 2 - 5.2x \\ 3.2 - 0.5x - 2x &= 4.8x + 2 - 5.2x \\ 3.2 - 2.5x &= -0.4x + 2 \\ -3.2 + 0.4x & \quad +0.4x - 3.2 \\ \hline -2.1x &= -1.2 \\ \frac{-2.1x}{2.1} &= \frac{-1.2}{2.1} \\ x &= -0.57 \end{aligned}$$

Answer $x = \underline{-0.57}$

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. An error is made when distributing $(-0.5(x + 4) \neq -0.5x - 2x)$. The final division should be a division by -2.1 on both sides, which would make the solution positive. The solution is inappropriately rounded.

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation _____

State your reason.

Nonlinear equation _____

State your reason.

EXEMPLARY RESPONSE

48

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation $y = \frac{x}{3} + 2$ or $y = 2 - 3x$

State your reason.

The equation is linear if x has an exponent of 0 or 1. In either equation x has an exponent of 1.

or

The equation is in the $y = mx + b$ format, which is a standard linear form.

or

When graphed, a straight line is drawn.

or other valid reason

Nonlinear equation $y = x(3x + 2)$

State your reason.

The equation $y = x(3x + 2)$ is a quadratic equation, which is nonlinear, and its graph is a parabola (curve). When substituting values into this equation for x , the function does not increase at a constant rate.

x	y
0	0
1	5
2	16

or other valid reason

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation $y = \frac{x}{3} + 2$

State your reason.

x is to the first power, if it
is to the first power it is a
linear equation, (the highest degree of x is 1)

Nonlinear equation $y = x(3x + 2)$

State your reason.

$y = x(3x + 2) = y = 3x^2 + 2x$, this is a
nonlinear equation because x is to
the second power (the highest degree of

Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. A correct linear equation is chosen, and a correct explanation is provided. A correct nonlinear equation is chosen, and a correct explanation is provided. This response is complete and correct.

GUIDE PAPER 2

48

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation

$$y = \frac{x}{3} + 2$$

State your reason.

The x's power goes to 1 which makes it linear.

Nonlinear equation

$$y = x(3x + 2)$$

State your reason.

When you distribute the x it will be x^2 and for the equation to be linear the x has to be to the power of 0 or 1.

Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. A correct linear equation is chosen, and a correct explanation is provided. A correct nonlinear equation is chosen, and a correct explanation is provided. This response is complete and correct.

GUIDE PAPER 3

48

Three equations are listed below.

- $y = x(3x + 2)$ $3x^2 + 2x$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why ~~each equation you identified~~ is linear or nonlinear.

Linear equation $2 - 3x$

State your reason.

The equation fits into $y = mx + b$ format, and has a negative line/slope

Nonlinear equation $x(3x + 2)$

State your reason.

It's a quadratic equation, due to the x being squared; the equation doesn't have a straight line.

Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts and procedures in the task. Correct equations are identified as linear and nonlinear, and the explanations are sufficient to show a thorough understanding. Writing expressions instead of equations is considered inconsequential.

GUIDE PAPER 4

48

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation $y = 2 - 3x$

State your reason.

It is in $y = mx + b$ form, so it is linear.

Nonlinear equation $y = x(3x + 2)$

State your reason.

The x will not be to the first power because $1x + 3x = 3x^2$, so it is not linear.

Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts and procedures in the task. Correct linear and nonlinear equations are identified. The explanation of the linear equation is correct, but the explanation of the nonlinear equation contains an incorrect statement. The variable x to the power of 0 is not addressed and will make an equation linear. This response appropriately addresses most but not all aspects of the task.

GUIDE PAPER 5

48

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation

$$y = 2 - 3x$$

State your reason.

The exponent on the x isn't a number other than 1 or 0.

Nonlinear equation

$$y = x(3x+2)$$

State your reason.

The x is being distributed.

Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts and procedures in the task. Correct linear and nonlinear equations are chosen. The explanation of the linear equation is correct and is understood to mean that the exponent on the x must be 1 or 0. The nonlinear equation is insufficiently explained. This response appropriately addresses most but not all aspects of the task.

GUIDE PAPER 6

48

Three equations are listed below.

• $y = x(3x + 2)$

• $y = \frac{x}{3} + 2$

• $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation $\frac{x}{3} + 2$

State your reason.

This equation has a constant rate of change.

Nonlinear equation $x(3x + 2)$

State your reason.

This equation does not have a constant rate of change.

Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts and procedures in the task. Correct linear and nonlinear equations are chosen. The explanations are not specific enough as they do not show how the rates of change are related to the algebraic forms of the equations. This response appropriately addresses most but not all aspects of the task.

GUIDE PAPER 7

48

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation $y = \frac{x}{3} + 2$

State your reason.

Because its written like a linear equation
is written ($y = mx + b$)

Nonlinear equation $y = 2 - 3x$

State your reason.

the x is on the end and it shouldn't
be.

Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts and procedures in the task. A correct linear equation is chosen with a valid explanation. An incorrect nonlinear equation is chosen, and an incorrect explanation is provided. This response reflects a lack of essential understanding.

48

Three equations are listed below.

- $y = x(3x + 2)$

- $y = \frac{x}{3} + 2$

- $y = 2 - 3x$

$$y = 3x^2 + 7$$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation $y = 2 - 3x$

State your reason.

 The equation is linear because it
 is not exponential

Nonlinear equation $y = x(3x + 2)$

State your reason.

 The equation is exponential
 is

Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts and procedures in the task. Correct linear and nonlinear equations are chosen. The explanations are not completely accurate, but holistically, there is some understanding that an exponential equation is nonlinear. This response reflects a lack of essential understanding.

GUIDE PAPER 9

48

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation

$y = 2 - 3x$ is linear.

State your reason.

because it has an exponent of 1 or zero.

Nonlinear equation

$y = x/3 + 2$

State your reason.

because the x is a fraction.

Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts and procedures in the task. A correct linear equation is chosen. The explanation of the linear equation does not make it clear that the exponent is attached to a variable, but correctly identifies the exponent as being only 1 or 0. An incorrect nonlinear equation is chosen, and an incorrect explanation is provided. This response reflects a lack of essential understanding.

GUIDE PAPER 10

48

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation

$$y=2-3x$$

State your reason.

because it fits in to the equation format, $y=mx+b$
 $y=2-3x$ and there is a solution

Nonlinear equation

$$y=x/3+2$$

State your reason.

it has a fraction and has to be divided and cannot be plugged in to fit a graph.

Score Point 0 (out of 3 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. Although a correct linear equation is chosen, the explanation does not clearly identify $y = mx + b$ as linear, and inappropriately suggests that having a solution is important for determining linearity. An incorrect nonlinear equation is chosen, and an incorrect explanation is provided.

Three equations are listed below.

- $y = x(3x + 2)$
- $y = \frac{x}{3} + 2$
- $y = 2 - 3x$

Identify one linear equation and one nonlinear equation from the list. State a reason why each equation you identified is linear or nonlinear.

Linear equation $y = x(3x + 2)$ _____

State your reason.

Because it goes in a straight line
I think.

Nonlinear equation $y = \frac{x}{3} + 2$ _____

State your reason.

Because it does not go
straight.

Score Point 0 (out of 3 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. Incorrect linear and nonlinear equations are chosen, so even though the reasons convey the concept of linearity, holistically, this response shows no overall understanding.

