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## Our Students. Their Moment.

# New York State Regents Examination in Geometry (Common Core) 

Performance Level Descriptions

August 2015

## Geometry Performance Level Descriptions

## Policy-Level Performance Level Definitions

For each subject area, there are students performing along a proficiency continuum with regard to the skills and knowledge necessary to meet the demands of Common Core Learning Standards for Mathematics. There are students who are exceed the expectations of the standards, students meet the expectations, students who partially meet the expectations, and students who do not demonstrate sufficient knowledge or skills required for any performance level. New York State assessments are designed to classify students into one of four proficiency categories; these proficiency categories are defined as:

## NYS Level 5

Students performing at this level exceed Common Core expectations.

## NYS Level 4

Students performing at this level meet Common Core expectations.

## NYS Level 3

Students performing at this level partially meet Common Core expectations (required for current Regents Diploma purposes).

## NYS Level 2 (Safety Net)

Students performing at this level partially meet Common Core expectations (required for Local Diploma purposes).

## NYS Level 1

Students performing at this level do not demonstrate the knowledge and skills required for NYS Level 2.

## Performance Level Descriptions

Performance Level Descriptions (PLDs) describe the range of knowledge and skills students should demonstrate at a given performance level.

## How were the PLDs developed?

The New York State Education Department (NYSED) convened the state's English Language Arts (ELA) and Math Content Advisory Panels (CAPs) to develop the initial draft PLDs for Algebra I and English Language Arts. The CAPs are classroom teachers from elementary, middle and high school, school and district administrators, English Language Learner (ELL) and students with disabilities (SWD) specialists, and higher education faculty members from across the state.

The draft PLDs from the CAPs then went through additional rounds of review and edit from a number of NYS-certified educators, content specialists, and assessment experts under NYSED supervision. In developing PLDs, participants considered policy-level definitions of the performance levels (see above) and the expectations for each grade level in the Common Core Learning Standards.

## How are the PLDs used in Assessment?

PLDs are essential in setting standards for the New York State Regents Examinations. Standard setting panelists use PLDs to determine the threshold expectations for students to demonstrate the knowledge and skills necessary to attain just barely a Level 2, Level 3, Level 4, or Level 5 on the assessment. These discussions then influence the panelists in establishing the cut scores on the assessment. PLDs are also used to inform item development, as each test needs questions that distinguish performance all along the continuum.

## How can the PLDs be used in Instruction?

PLDs help communicate to students, families, educators and the public the specific knowledge and skills expected of students to demonstrate proficiency and can serve a number of purposes in classroom instruction. They are the foundation of rich discussion around what students need to do to perform at higher levels and to explain the progression of learning within a subject area. We encourage the use of the PLDs for a variety of purposes, such as differentiating instruction to maximize individual student outcomes, creating classroom assessments and rubrics to help in identifying target performance levels for individual or groups of students, and tracking student growth along the proficiency continuum as described by the PLDs. In order to facilitate the use of the PLDs in instruction, the skills differentiating performance levels have been identified using bold text.

| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Congruence <br> (G-CO) | Use precise language to <br> describe a sequence of <br> rigid motions to <br> determine the <br> congruency of figures. | Describe a sequence of <br> rigid motions to <br> determine the <br> congruency of figures. | Identify and draw a <br> sequence of rigid <br> motions in the plane to <br> verify the congruency <br> of figures. | Identify and draw a rigid <br> motion in the plane. | Sketch triangles and <br> rectangles. |
|  | Use precise language to <br> predict the effect of a <br> given rigid motion on a <br> given figure. | Predict the effect of a <br> given rigid motion on a <br> given figure. | Identify the image and <br> describe the effect of a <br> given rigid motion. | Identify the image of a <br> given rigid motion. |  |
|  | Formulate a complete <br> line of geometric <br> reasoning to prove a <br> geometric theorem. | Formulate a complete <br> line of geometric <br> reasoning to prove a <br> specific geometric <br> statement. | Formulate a partial line <br> of geometric reasoning in <br> an effort to prove a <br> specific geometric <br> statement. | Provide a correct <br> geometric statement <br> pertaining to the given <br> geometric information. | Rentext of a proof. <br> information in the <br> conte |
|  | Use the rotations and <br> reflections that carry a <br> figure onto itself to prove <br> or explain if the figure is <br> or is not regular. | Describe the rotations <br> and reflections that carry <br> a figure onto itself. | Identify the rotations and <br> reflections that carry a <br> figure onto itself. |  |  |
|  | Determine the validity of <br> geometric arguments and <br> revise invalid geometric <br> arguments. | Determine the validity of <br> geometric arguments <br> with justification. | Determine the validity of <br> geometric arguments. |  |  |


| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| (G-CO <br> continued) | Make advanced formal <br> geometric constructions <br> using appropriate tools. | Construct the <br> application of the listed <br> constructions, for <br> example, using the <br> construction of a <br> midpoint to construct the <br> median of a triangle or <br> construct the dilation of a <br> figure not on the <br> coordinate plane. | Make basic formal <br> geometric constructions <br> using appropriate tools. <br> Examples of basic <br> constructions include but <br> are not limited to: copy a <br> segment, bisecting a <br> segment, bisecting an <br> angle. | Construct rays, <br> triangles, and angles. <br> line segments. |  |


| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Similarity, <br> Right <br> Triangles, and <br> Trigonometry <br> (G-SRT) | Use precise language to <br> describe a sequence of <br> similarity <br> transformations to <br> determine the similarity <br> of figures. | Describe a sequence of <br> similarity <br> transformations to <br> determine the similarity <br> of figures. | Identify a sequence of <br> similarity <br> transformations in the <br> plane to verify the <br> similarity of figures. | Perform a dilation in the <br> coordinate plane <br> centered at the origin. <br> Distinguish between a <br> dilation and a <br> translation, reflection, or <br> rotation. |  |
|  | Formulate a complete <br> line of geometric <br> reasoning to prove a <br> geometric theorem. | Formulate a complete <br> line of geometric <br> reasoning to prove a <br> specific geometric <br> statement. | Formulate a partial line <br> of geometric reasoning in <br> an effort to prove a <br> specific geometric <br> statement. | Provide correct <br> geometric statements <br> pertaining to the given <br> geometric information. | Restate given <br> information in the <br> context of a proof. |

Geometry (Common Core) Performance Level Descriptions

| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| (G-SRT <br> continued) | Apply congruence or <br> similarity criteria to solve <br> complex problems <br> involving multiple <br> concepts, and explain the <br> geometric reasoning <br> involved. | Apply congruence or <br> similarity criteria to solve <br> problems, and explain <br> the geometric reasoning <br> involved. | Apply congruence or <br> similarity criteria to solve <br> problems. | Apply congruence or <br> similarity criteria to <br> solve simple problems. |  |
|  |  | Use the Pythagorean <br> Theorem, trigonometric <br> ratios, and the <br> relationship between sine <br> and cosine of <br> complementary angles to <br> solve complex <br> problems. | Use the Pythagorean <br> Theorem, trigonometric <br> ratios, and the <br> relationship between <br> sine and cosine of <br> complementary angles <br> to solve problems. | Identify the <br> trigonometric ratios of a <br> right triangle. | Sketch and label the <br> sides of right <br> triangles. |
|  |  | Determine the validity of <br> geometric arguments and <br> revise invalid geometric <br> arguments. | Determine the validity of <br> geometric arguments <br> with justification. | Determine the validity of <br> geometric arguments. |  |


| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Circles <br> (G-C) | Use appropriate tools to <br> construct the inscribed <br> and circumscribed circle <br> for a given triangle and <br> justify the construction. | Use appropriate tools to <br> construct the inscribed <br> and circumscribed circle <br> for a given triangle. | Use appropriate tools to <br> construct the <br> circumscribed circle for <br> a given triangle. |  |  |
|  | Derive the formula for <br> the arc length and area of <br> a sector. | Apply formulas for arc <br> length and area of a <br> sector to solve complex <br> problems. | Determine the arc length <br> and area of a sector given <br> any central angle in <br> degrees or radians. | Determine the area of a <br> quarter, half, or three- <br> quarter circle, given the <br> area of the entire circle. | Write an expression <br> for the area of a <br> circle given the <br> radius. |

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| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| (G-C <br> continued) |  | Apply theorems about <br> arcs, angles, and <br> segments related to <br> circles. | Apply theorems about <br> arcs and angles related to <br> circles. | Identify arcs, angles, <br> and segments related to <br> circles. | Visually compare <br> central angle <br> measures. |
|  |  | Explain the radian <br> measure of a central <br> angle as the constant of <br> proportionality between <br> the arc length and the <br> radius of a circle. | Identify central angles in <br> different circles that have <br> the same radian measure. |  |  |
|  |  | Formulate a complete <br> line of geometric <br> reasoning to prove <br> properties of angles for a <br> quadrilateral inscribed in <br> a circle. | Formulate a partial line <br> of geometric reasoning in <br> an effort to prove <br> properties of angles for a <br> quadrilateral inscribed in <br> a circle. | Identify a missing angle <br> in a diagram involving a <br> quadrilateral inscribed <br> in a circle. |  |
|  | Formulate a complete <br> line of geometric <br> reasoning to prove that <br> circles are similar. | Formulate a partial line <br> of geometric reasoning in <br> an effort to prove that <br> circles are similar. | Find missing radius and <br> circumference <br> measurements using <br> circle similarity. |  |  |


| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Expressing <br> Geometric <br> Properties <br> with <br> Equations <br> (G-GPE) | Use the Pythagorean theorem to derive the equation of a circle. | Given the equation of a circle in standard form, complete the square to obtain the center and radius. | Identify the center and radius of a circle when given the equation in center-radius form. | Complete the square with a single variable. |  |
|  | Use coordinates to formulate a complete line of geometric reasoning to prove or disprove a geometric theorem. | Use coordinates to formulate a complete line of geometric reasoning to prove a specific geometric statement. | Use numerical coordinates to formulate a partial line of geometric reasoning in an effort to prove a specific geometric statement. | Given three coordinates of a special quadrilateral, determine the fourth coordinate. |  |
|  | Explain why parallel lines have the same slopes and perpendicular lines have negative reciprocal slopes. | Use the slope criteria for parallel and perpendicular lines to solve geometric problems. | Identify the equations of lines as parallel, perpendicular, or neither. | Identify the slope of a line given its equation. | Distinguish between lines in a coordinate plane with positive and negative slopes. |
|  |  | Identify the rational coordinates of a point that divides a segment into a given ratio. | Identify the whole number coordinates of a point that divides a segment into a given ratio. | Identify the coordinates of the midpoint of a line segment. | Locate the midpoint of a horizontal or vertical line in a coordinate plane. |

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| :--- | :--- | :--- | :--- | :--- | :--- |
| $\begin{array}{l}\text { (G-GPE } \\ \text { continued) }\end{array}$ | $\begin{array}{l}\text { Use coordinates to } \\ \text { compute perimeters and } \\ \text { areas of compound } \\ \text { figures. }\end{array}$ | $\begin{array}{l}\text { Use coordinates to } \\ \text { compute perimeters of } \\ \text { polygons and areas of } \\ \text { triangles and rectangles } \\ \text { with rational or } \\ \text { irrational bases and } \\ \text { heights. }\end{array}$ | $\begin{array}{l}\text { Use coordinates to } \\ \text { compute perimeters of } \\ \text { polygons with rational } \\ \text { side lengths. } \\ \text { Use coordinates to } \\ \text { compute areas of } \\ \text { triangles and rectangles } \\ \text { with rational bases and } \\ \text { heights. }\end{array}$ | $\begin{array}{l}\text { Compute the length of } \\ \text { vertical, horizontal, and } \\ \text { diagonal segments on } \\ \text { the coordinate plane } \\ \text { with integer coordinates. } \\ \text { Compute the perimeter } \\ \text { of polygons with integer } \\ \text { side lengths in the } \\ \text { coordinate plane. } \\ \text { Compute the area of } \\ \text { triangles and rectangles } \\ \text { number coordinates } \\ \text { rectangles } .\end{array}$ |  |
| with integer bases and |  |  |  |  |  |$\}$


| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Geometric <br> Measurement <br> \& Dimensions <br> (G-GMD) | Write a formal <br> argument for the <br> formulas for the <br> circumference of a circle, <br> area of a circle, and <br> volumes of a cylinder, <br> pyramid, and cone. | Write an informal <br> argument for the <br> formulas for the <br> circumference of a circle, <br> area of a circle, and <br> volumes of a cylinder, <br> pyramid, and cone. |  |  |  |
|  | Use the volume formulas <br> for cylinders, pyramids, <br> cones, and spheres to <br> solve modeling <br> problems involving <br> compound figures. | Use the volume formulas <br> for cylinders, pyramids, <br> cones, and spheres to <br> solve modeling <br> problems. | Use the volume formulas <br> for cylinders, pyramids, <br> cones, and spheres to <br> find various dimensions <br> of the solid, such as <br> finding the radius of a <br> sphere given the volume. | Compute the volumes <br> for cylinders, cones, and <br> spheres. | Compute the <br> volume of a <br> rectangular prism <br> with integer <br> dimensions. |

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| :--- | :--- | :--- | :--- | :--- | :--- |
| (G-GMD <br> continued) | Describe the similarities <br> and differences between <br> various cross-sections of <br> three-dimensional <br> objects, such as <br> explaining the difference <br> between the areas of <br> different cross-sections <br> of the same figure. | Describe the two- <br> dimensional cross- <br> sections of three- <br> dimensional objects. | Identify the two- <br> dimensional cross- <br> sections using a diagram <br> of a three-dimensional <br> object. | Identify a two- <br> dimensional cross- <br> section that results from <br> slicing a right <br> rectangular prism or a <br> right rectangular <br> pyramid. | Identify the shape <br> of the base of a <br> rectangular prism, <br> triangular prism, or <br> cylinder. |
|  | Describe the similarities <br> and differences between <br> various rotations of <br> two-dimensional <br> objects, such as a half <br> rotation or rotating about <br> different axes. | Describe three- <br> dimensional objects <br> generated by rotations of <br> two-dimensional objects. | Identify three- <br> dimensional objects <br> generated by rotations of <br> two-dimensional objects. |  |  |


| Domain | NYS Level 5 | NYS Level 4 | NYS Level 3 | NYS Level 2 | NYS Level 1 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Modeling with <br> Geometry <br> (G-MG) | Create a model to solve <br> real-world problems, <br> which may include <br> applying density to real- <br> world situations or <br> solving design problems. | Apply geometric <br> concepts in modeling <br> situations to solve <br> complex real-world <br> problems, which may <br> include applying density <br> to real-world situations <br> or solving design <br> problems. | Apply concepts of <br> density to solve a <br> problem that may <br> include converting <br> between two- and three- <br> dimensional units. | Given two of the three <br> values in the density <br> formula, find the third <br> value. | Compute the area of <br> a rectangular <br> region, given whole <br> number dimensions. |

